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# Data structure

## Fenwick tree

template<typename T>

struct fenwick\_tree {

/\* can convert it to map

\* build what you need only

\* will be: memory O(q\*logn) ,time O(logn\*logn) \*/

vector<T> BIT;

int n;

fenwick\_tree(int n) :

n(n), BIT(n + 1) {

}

T getAccum(int idx) {

T sum = 0;

while (idx) {

sum += BIT[idx];

idx -= (idx & -idx);

}

return sum;

}

void add(int idx, T val) {

assert(idx != 0);

while (idx <= n) {

BIT[idx] += val;

idx += (idx & -idx);

}

}

T getValue(int idx) {

return getAccum(idx) - getAccum(idx - 1); }

// ordered statistics tree

// get index that has value >= accum

// values must by positive

int getIdx(T accum) {

int start = 1, end = n, rt = -1;

while (start <= end) {

int mid = start + end >> 1;

T val = getAccum(mid);

if (val >= accum)

rt = mid, end = mid - 1;

else

start = mid + 1;

}

return rt;

}

//need review (from topcoder)

//first index less than or equal accum O(logn)

int find(T accum) { //equal getIdx

int i = 1, idx = 0;

while ((1 << i) <= MAX)

i <<= 1;

for (idx = 0; i > 0; i >>= 1) {

int tidx = idx + i;

if (tidx > MAX)

continue;

if (accum >= BIT[tidx]) {

idx = tidx;

accum -= BIT[tidx];

}

}

return idx;//idx+1 if you need first greater

}

};

### Fenwick tree 2d

template<typename T>

struct fenwick\_tree\_2d {

#define Lbit(x) (x&-x)

int n, m;

vector<vector<T>> BIT;

fenwick\_tree\_2d(int n, int m) :

n(n), m(m), BIT(n + 1, vector<T>(m + 1)) {

}

T getAccum(int i, int j) {

T sum = 0;

for (; i; i -= Lbit(i))

for (int idx = j; idx > 0; idx -= Lbit(idx))

sum += BIT[i][idx];

return sum;

}

void add(int i, int j, int val) {

assert(i != 0 && j != 0);

for (; i <= n; i += Lbit(i))

for (int idx = j; idx <= m; idx += Lbit(idx))

BIT[i][idx] += val;

}

T getRectangeSum(int x1, int y1, int x2, int y2) {

if (y1 > y2)

swap(y1, y2);

if (x1 > x2)

swap(x1, x2);

return getAccum(x2, y2) - getAccum(x1 - 1, y2) - getAccum(x2, y1 - 1)

+ getAccum(x1 - 1, y1 - 1);

}

};

### Fenwick tree max

//fenwick tree for get maximum from 1 to idx

// update a[idx] = max(a[idx],val)

//can't remove values

template<typename T>

struct fenwick\_tree {

vector<T> BIT;

int n;

fenwick\_tree(int n) :

n(n), BIT(n + 1) {

}

T getMax(int idx) {

T mx = numeric\_limits<T>::min();

while (idx) {

mx = max(mx, BIT[idx]);

idx -= (idx & -idx);

}

return mx;

}

void add(int idx, T val) {

assert(idx != 0);

while (idx <= n) {

BIT[idx] = max(BIT[idx], val);

idx += (idx & -idx);

}

}

};

### Fenwick tree update range

/\*

x[i] = a[i] - a[i-1] //a is original array

y[i] = x[i]\*(i-1)

sum(1,3) = a[1] + a[2] + a[3] = (x[1]) + (x[2] + x[1]) + (x[3] + x[2] + x[1])

= 3\*(x[1] + x[2] + x[3]) - 0\*x[1] - 1\*x[2] - 2\*x[3] //same equation but more complex

= sumX(1,3) \* 3 - sumY(1,3)

so sum(1,n) = sumX(1,n)\*n - sumY(1,n)

update:

x[l] += val,x[r+1] -= val

y[l] += val \*(l-1),y[r+1] -= r\*val

\*/

template<typename T>

class fenwick\_tree {

int n;

vector<T> x, y;

T getAccum(vector<T>& BIT, int idx) {

T sum = 0;

while (idx) {

sum += BIT[idx];

idx -= (idx & -idx);

}

return sum;

}

void add(vector<T>& BIT, int idx, T val) {

assert(idx != 0);

while (idx <= n) {

BIT[idx] += val;

idx += (idx & -idx);

}

}

T prefix\_sum(int idx) {

return getAccum(x, idx) \* idx - getAccum(y, idx);

}

public:

fenwick\_tree(int n) :

n(n), x(n + 1), y(n + 1) {

}

void update\_range(int l, int r, T val) {

add(x, l, val);

add(x, r + 1, -val);

add(y, l, val \* (l - 1));

add(y, r + 1, -val \* r);

}

T range\_sum(int l, int r) {

return prefix\_sum(r) - prefix\_sum(l - 1);

}

};

## Segment tree

/\*

for efficient memory (2\*n)

#define LEFT (idx+1)

#define MID ((start+end)>>1)

#define RIGHT (idx+((MID-start+1)<<1))

\*/

template<typename node> class segment\_tree {

#define LEFT (idx<<1)

#define RIGHT (idx<<1|1)

#define MID ((start+end)>>1)

int left\_range, right\_range;

vector<node> tree;

inline void pushup(int idx) {

tree[idx] = node(tree[LEFT], tree[RIGHT]);

}

inline void pushdown(int idx, int start, int end) {

if (!tree[idx].have\_lazy || start == end)

return;

tree[LEFT].apply(start, MID, tree[idx].lazy\_value);

tree[RIGHT].apply(MID + 1, end, tree[idx].lazy\_value);

tree[idx].clear\_lazy();

}

void build(int idx, int start, int end) {

if (start == end)

return;

build(LEFT, start, MID);

build(RIGHT, MID + 1, end);

pushup(idx);

}

template<typename T>

void build(int idx, int start, int end, const vector<T>& arr) {

if (start == end) {

tree[idx] = arr[start];

return;

}

build(LEFT, start, MID, arr);

build(RIGHT, MID + 1, end, arr);

pushup(idx);

}

node query(int idx, int start, int end, int from, int to) {

if (from <= start && end <= to)

return tree[idx];

pushdown(idx, start, end);

if (to <= MID)

return query(LEFT, start, MID, from, to);

if (MID < from)

return query(RIGHT, MID + 1, end, from, to);

return node(query(LEFT, start, MID, from, to),

query(RIGHT, MID + 1, end, from, to));

}

template<typename ... T>

void update(int idx, int start, int end, int from, int to,const T&... val) {

if (to < start || end < from)

return;

if (from <= start && end <= to) {

tree[idx].apply(start, end, val...);

return;

}

pushdown(idx, start, end);

update(LEFT, start, MID, from, to, val...);

update(RIGHT, MID + 1, end, from, to, val...);

pushup(idx);

}

void init(int l, int r) {

left\_range = l;

right\_range = r;

tree = vector < node >((r - l + 1) << 2);

}

public:

segment\_tree(int l, int r) {

init(l, r);

build(1, l, r);

}

template<typename T>

segment\_tree(int l, int r, const vector<T>& v) {

init(l, r);

build(1, l, r, v);

}

node query(int l, int r) {

assert(left\_range <= l && l <= r && r <= right\_range);

return query(1, left\_range, right\_range, l, r);

}

template<typename ... T>

void update(int l, int r, const T&... val) {

assert(left\_range <= l && l <= r && r <= right\_range);

update(1, left\_range, right\_range, l, r, val...);

}

#undef LEFT

#undef RIGHT

#undef MID

};

### Iterative Segment tree

struct node {

node() { //set Default value

}

node(const node& a, const node& b) {}

void apply(int val) {}

};

struct segment\_tree {

int n; //0 to n-1

vector<node> tree;

segment\_tree(int n) {

resize(n);

build();

}

template<typename T>

segment\_tree(const vector<T>& arr) {

resize(arr.size());

for (int i = 0; i < arr.size(); i++)

tree[n + i] = arr[i];

build();

}

void resize(int n) {

int p = 1;

while (p < n)

p <<= 1;

this->n = p;

tree = vector < node >(p << 1);

}

void build() {

for (int i = n - 1; i > 0; i--)

tree[i] = node(tree[i << 1], tree[i << 1 | 1]);

}

template<typename T>

void update(int p, const T& value) {

tree[p += n].apply(value);

for (int i = p / 2; i > 0; i >>= 1)

tree[i] = node(tree[i << 1], tree[i << 1 | 1]);

}

node query(int l, int r) { //[l, r]

node resl, resr; //set default value in node

for (l += n, r += n + 1; l < r; l >>= 1, r >>= 1) {

if (l & 1) {

resl = node(resl, tree[l]);

l++;

}

if (r & 1) {

r--;

resr = node(tree[r], resr);

}

}

return node(resl, resr);

}

int kth\_one(int k, int i = 1) {

if (k > tree[i])

return -1;

if (i >= n)

return i - n;

if (tree[i << 1] >= k)

return kth\_one(k, i << 1);

return kth\_one(k - tree[i << 1], i << 1 | 1);

}

};

### Max sum range node

struct MSR\_Node {

ll left, right, mid, sum;

MSR\_Node(const ll& val) {

left = right = mid = sum = val;

}

MSR\_Node(const MSR\_Node& a, const MSR\_Node& b) {

left = max(a.left, a.sum + b.left);

right = max(b.right, b.sum + a.right);

mid = max({ a.mid, b.mid, a.right + b.left });

sum = a.sum + b.sum;

}

ll getMax() {

return max({ left, right, mid, sum });

}

};

### Persistent segment tree

struct segtree {

    static segtree \*sentinel;

    segtree \*left, \*right;

    bool dirty = false;

    ll sum = 0;

    ll lazy = 0;

    segtree(ll val = 0) :

            sum(val) {

        left = right = this;

    }

    segtree(segtree \*left, segtree \*right) :

            left(left), right(right) {

        sum = left->sum + right->sum;

    }

};

segtree \*segtree::sentinel = new segtree();

class persistent\_segment\_tree {

#define MID ((start+end)>>1)

    segtree\* apply(segtree \*root, int start, int end, ll val) {

        segtree \*rt = new segtree(\*root);

        rt->dirty = true;

        rt->sum += (end - start + 1) \* val;

        rt->lazy += val;

        return rt;

    }

    void pushdown(segtree \*root, int start, int end) {

        if (root->dirty == false || start == end)

            return;

        root->left = apply(root->left, start, MID, root->lazy);

        root->right = apply(root->right, MID + 1, end, root->lazy);

        root->lazy = 0;

        root->dirty = 0;

    }

    segtree\* build(int start, int end, const vector<int> &v) {

        if (start == end)

            return new segtree(v[start]);

        return new segtree(build(start, MID, v), build(MID + 1, end, v));

    }

    segtree\* Set(segtree \*root, int start, int end, int pos, ll new\_val) {

        pushdown(root, start, end);

        if (pos < start || end < pos)

            return root;

        if (pos <= start && end <= pos)

            return new segtree(new\_val);

        return new segtree(Set(root->left, start, MID, pos, new\_val),

                Set(root->right, MID + 1, end, pos, new\_val));

    }

    segtree\* update(segtree \*root, int start, int end, int l, int r, ll val) {

        pushdown(root, start, end);

        if (r < start || end < l)

            return root;

        if (l <= start && end <= r)

            return apply(root, start, end, val);

        return new segtree(update(root->left, start, MID, l, r, val),

                update(root->right, MID + 1, end, l, r, val));

    }

    ll query(segtree \*root, int start, int end, int l, int r) {

        pushdown(root, start, end);

        if (r < start || end < l)

            return 0;

        if (l <= start && end <= r)

            return root->sum;

        return query(root->left, start, MID, l, r)

                + query(root->right, MID + 1, end, l, r);

    }

public:

    int start, end;

    vector<segtree\*> versions;

    persistent\_segment\_tree(int start, int end) :

            start(start), end(end) {

        versions.push\_back(segtree::sentinel);

    }

    persistent\_segment\_tree(const vector<int> &v) :

            start(0), end(v.size() - 1) {

        versions.push\_back(build(start, end, v));

    }

    void update(int l, int r, ll val) {

        versions.push\_back(update(versions.back(), start, end, l, r, val));

    }

    ll query(int time, int l, int r) {

        return query(versions[time], start, end, l, r);

    }

#undef MID

};

### Extended Segment tree

struct segtree {

    segtree \*left = nullptr, \*right = nullptr;

    int mx = 0;

    segtree(int val = 0) :

            mx(val) {

    }

    void extend() {

        if (left == NULL) {

            left = new segtree();

            right = new segtree();

        }

    }

    void pushup() {

        mx = max(left->mx, right->mx);

    }

};

class extened\_segment\_tree {

#define MID ((start+end)>>1)

    void update(segtree \*root, int start, int end, int pos, int val) {

        if (pos < start || end < pos)

            return;

        if (start == end) {

            root->mx = max(root->mx, val);

            return;

        }

        root->extend();

        update(root->left, start, MID, pos, val);

        update(root->right, MID + 1, end, pos, val);

        root->pushup();

    }

    int query(segtree \*root, int start, int end, int l, int r) {

        if (root == nullptr || r < start || end < l)

            return 0;

        if (l <= start && end <= r)

            return root->mx;

        return max(query(root->left, start, MID, l, r),

                query(root->right, MID + 1, end, l, r));

    }

public:

    int start, end;

    segtree \*root;

    extened\_segment\_tree() {

    }

    extened\_segment\_tree(int start, int end) :

            start(start), end(end) {

        root = new segtree();

    }

    void update(int pos, int val) {

        update(root, start, end, pos, val);

    }

    int query(int l, int r) {

        return query(root, start, end, l, r);

    }

#undef MID

};

## Ordered set

#include<bits/stdc++.h>

#include<ext/pb\_ds/assoc\_container.hpp>

#include<ext/pb\_ds/tree\_policy.hpp>

using namespace std;

using namespace \_\_gnu\_pbds;

template<typename key>

using ordered\_set = tree<key, null\_type, less<key>, rb\_tree\_tag, tree\_order\_statistics\_node\_update>;

/\*

find\_by\_order(k) :

It returns to an iterator to the k-th element (counting from zero) in the set in O(logn) time.

To find the first element k must be zero.

order\_of\_key(k) :

It returns to the number of items that are strictly smaller than our item k in O(logn) time.

\*/

## Sparse table

template<typename T>

struct sparse\_table {

vector<vector<T>> sparseTable;

using F = function<T(T, T)>;

F merge;

static int LOG2(int x) { //floor(log2(x))

return 31 - \_\_builtin\_clz(x);

}

sparse\_table(vector<T>& v, F merge) :

merge(merge) {

int n = v.size();

int logN = LOG2(n);

sparseTable = vector<vector<T>>(logN + 1);

sparseTable[0] = v;

for (int k = 1, len = 1; k <= logN; k++, len <<= 1) {

sparseTable[k].resize(n);

for (int i = 0; i + len < n; i++)

sparseTable[k][i] = merge(sparseTable[k - 1][i],

sparseTable[k - 1][i + len]);

}

}

T query(int l, int r) {

int k = LOG2(r - l + 1); // max k ==> 2^k <= length of range

//check first 2^k from left and last 2^k from right //overlap

return merge(sparseTable[k][l], sparseTable[k][r - (1 << k) + 1]);

}

T query\_shifting(int l, int r) {

T res;

bool first = true;

for (int i = (int)sparseTable.size() - 1; i >= 0; i--)

if (l + (1 << i) - 1 <= r) {

if (first)

res = sparseTable[i][l];

else

res = merge(res, sparseTable[i][l]);

first = false;

l += (1 << i);

}

return res;

}

};

## SQRT Decomposition

//zero based SQRT\_Decomposition with lazy propagation

template<typename update\_type, typename query\_type>

class SQRT\_Decomposition {

struct Bucket {

int l, r;

update\_type lazy;

Bucket(int l, int r) :

l(l), r(r) {

//set default value to lazy

//build bucket for the first time

}

void build() {

//update all bucket with lazy if have

//rebuild the bucket

//clear lazy

}

//update all bucket

void update(const update\_type& val) {

//just update lazy

}

//update range in bucket

void update(int start, int end, const update\_type& val) {

if (start == l && end == r) {

update(val);

return;

}

//update bucket

//rebuild the bucket if need

}

//query about all bucket

query\_type query() {

//calc with lazy

}

//query about range in bucket

query\_type query(int start, int end) {

if (start == l && end == r)

return query();

//push lazy if have

//calc

}

};

int n, sqrtN;

vector<Bucket> bucket;

int begin(int idx) {

return idx \* sqrtN;

}

int end(int idx) {

return min(sqrtN \* (idx + 1), n) - 1;

}

int which\_block(int idx) {

return idx / sqrtN;

}

public:

SQRT\_Decomposition(int n) {

this->n = n;

sqrtN = sqrt(n);

for (int i = 0; i < n; i += sqrtN)

bucket.push\_back(Bucket(i, min(i + sqrtN, n) - 1));

}

void update(int left, int right, update\_type val) {

int st = which\_block(left), ed = which\_block(right);

bucket[st].update(left, min(bucket[st].r, right), val);

for (int i = st + 1; i < ed; i++)

bucket[i].update(val);

if (st != ed)

bucket[ed].update(bucket[ed].l, right, val);

}

query\_type query(int left, int right) {

int st = which\_block(left), ed = which\_block(right);

query\_type rt = bucket[st].query(left, min(bucket[st].r, right));

for (int i = st + 1; i < ed; i++)

rt += bucket[i].query();

if (st != ed)

rt += bucket[ed].query(bucket[ed].l, right);

return rt;

}

};

## **Implicit** treap

enum DIR {

L, R

};

template<typename T>

struct cartesian\_tree {

static cartesian\_tree<T>\* sentinel;

T key;

int priority = 0, size = 0;

bool reverse = false;

cartesian\_tree\* child[2];

cartesian\_tree() {

key = T();

priority = 0;

child[L] = child[R] = this;

}

cartesian\_tree(const T& x, int y) :

key(x), priority(y) {

size = 1;

child[L] = child[R] = sentinel;

}

void push\_down() {

if (!reverse)

return;

reverse = 0;

child[L]->doRevese();

child[R]->doRevese();

}

void doReverse() {

reverse ^= 1;

swap(child[L], child[R]);

}

void push\_up() {

size = child[L]->size + child[R]->size + 1;

}

};

template<typename T>

cartesian\_tree<T>\* cartesian\_tree<T>::sentinel = new cartesian\_tree<T>();

template<typename T, template<typename > class cartesian\_tree>

class implicit\_treap { //1 based

typedef cartesian\_tree<T> node;

typedef cartesian\_tree<T>\* nodeptr;

#define emptyNode cartesian\_tree<T>::sentinel

nodeptr root;

void split(nodeptr root, nodeptr& l, nodeptr& r, int firstXElment) {

if (root == emptyNode) {

l = r = emptyNode;

return;

}

root->push\_down();

if (firstXElment <= root->child[L]->size) {

split(root->child[L], l, root->child[L], firstXElment);

r = root;

}

else {

split(root->child[R], root->child[R], r,

firstXElment - root->child[L]->size - 1);

l = root;

}

root->push\_up();

}

nodeptr merge(nodeptr l, nodeptr r) {

l->push\_down();

r->push\_down();

if (l == emptyNode || r == emptyNode)

return (l == emptyNode ? r : l);

if (l->priority > r->priority) {

l->child[R] = merge(l->child[R], r);

l->push\_up();

return l;

}

r->child[L] = merge(l, r->child[L]);

r->push\_up();

return r;

}

vector<nodeptr> split\_range(int s, int e) { // [x<s,s<=x<=e,e<x]

nodeptr l, m, r, tmp;

split(root, l, tmp, s - 1);

split(tmp, m, r, e - s + 1);

return { l,m,r };

}

public:

implicit\_treap() :

root(emptyNode) {

}

int size() {

return root->size;

}

void insert(int pos, const T& key) {

nodeptr tmp = new node(key, rand());

nodeptr l, r;

split(root, l, r, pos - 1);

root = merge(merge(l, tmp), r);

}

void push\_back(const T& value) {

root = merge(root, new node(value, rand()));

}

T getByIndex(int pos) {

vector<nodeptr> tmp = split\_range(pos, pos);

nodeptr l = tmp[0], m = tmp[1], r = tmp[2];

T rt = m->key;

root = merge(merge(l, m), r);

return rt;

}

void erase(int pos) {

vector<nodeptr> tmp = split\_range(pos, pos);

nodeptr l = tmp[0], m = tmp[1], r = tmp[2];

delete m;

root = merge(l, r);

}

void cyclic\_shift(int s, int e) { //to the right

vector<nodeptr> tmp = split\_range(s, e);

nodeptr l = tmp[0], m = tmp[1], r = tmp[2];

nodeptr first, second;

split(m, first, second, e - s);

root = merge(merge(merge(l, second), first), r);

}

void reverse\_range(int s, int e) {

vector<nodeptr> tmp = split\_range(s, e);

nodeptr l = tmp[0], m = tmp[1], r = tmp[2];

m->reverse ^= 1;

root = merge(merge(l, m), r);

}

node range\_query(int s, int e) {

vector<nodeptr> tmp = split\_range(s, e);

nodeptr l = tmp[0], m = tmp[1], r = tmp[2];

node rt = \*m;

root = merge(merge(l, m), r);

return rt;

}

};

### Ordered multiset

enum DIR {

L, R

};

template<typename T>

struct cartesian\_tree {

static cartesian\_tree<T>\* sentinel;

T key;

int priority = 0, frequency = 0, size = 0;

cartesian\_tree\* child[2];

cartesian\_tree() {

key = T();

priority = 0;

child[L] = child[R] = this;

}

cartesian\_tree(const T& x, int y) :

key(x), priority(y) {

size = frequency = 1;

child[L] = child[R] = sentinel;

}

void push\_down() {

}

void push\_up() {

size = child[L]->size + child[R]->size + frequency;

}

};

template<typename T>

cartesian\_tree<T>\* cartesian\_tree<T>::sentinel = new cartesian\_tree<T>();

template<typename T>

void split(cartesian\_tree<T>\* root, T key, cartesian\_tree<T>\*& l,

cartesian\_tree<T>\*& r) {

if (root == cartesian\_tree<T>::sentinel) {

l = r = cartesian\_tree<T>::sentinel;

return;

}

root->push\_down();

if (root->key <= key) {

split(root->child[R], key, root->child[R], r);

l = root;

}

else {

split(root->child[L], key, l, root->child[L]);

r = root;

}

root->push\_up();

}

template<typename T>

cartesian\_tree<T>\* merge(cartesian\_tree<T>\* l, cartesian\_tree<T>\* r) {

l->push\_down();

r->push\_down();

if (l == cartesian\_tree<T>::sentinel || r == cartesian\_tree<T>::sentinel)

return (l == cartesian\_tree<T>::sentinel ? r : l);

if (l->priority > r->priority) {

l->child[R] = merge(l->child[R], r);

l->push\_up();

return l;

}

r->child[L] = merge(l, r->child[L]);

r->push\_up();

return r;

}

template<typename T, template<typename > class cartesian\_tree>

class treap {

typedef cartesian\_tree<T> node;

typedef node\* nodeptr;

#define emptyNode node::sentinel

nodeptr root;

void insert(nodeptr& root, nodeptr it) {

if (root == emptyNode) {

root = it;

}

else if (it->priority > root->priority) {

split(root, it->key, it->child[L], it->child[R]);

root = it;

}

else

insert(root->child[root->key < it->key], it);

root->push\_up();

}

bool increment(nodeptr root, const T& key) {

if (root == emptyNode)

return 0;

if (root->key == key) {

root->frequency++;

root->push\_up();

return root;

}

bool rt = increment(root->child[root->key < key], key);

root->push\_up();

return rt;

}

nodeptr find(nodeptr root, const T& key) {

if (root == emptyNode || root->key == key)

return root;

return find(root->child[root->key < key], key);

}

void erase(nodeptr& root, const T& key) {

if (root == emptyNode)

return;

if (root->key == key) {

if (--(root->frequency) == 0)

root = merge(root->child[L], root->child[R]);

}

else

erase(root->child[root->key < key], key);

root->push\_up();

}

T kth(nodeptr root, int k) {

if (root->child[L]->size >= k)

return kth(root->child[L], k);

k -= root->child[L]->size;

if (k <= root->frequency)

return root->key;

return kth(root->child[R], k - root->frequency);

}

int order\_of\_key(nodeptr root, const T& key) {

if (root == emptyNode)

return 0;

if (key < root->key)

return order\_of\_key(root->child[L], key);

if (key == root->key)

return root->child[L]->size;

return root->child[L]->size + root->frequency

+ order\_of\_key(root->child[R], key);

}

public:

treap() :

root(emptyNode) {

}

void insert(const T& x) {

if (increment(root, x)) //change it to find(x) to make it as a set

return;

insert(root, new node(x, rand()));

}

void erase(const T& x) {

erase(root, x);

}

bool find(const T& x) {

return (find(root, x) != emptyNode);

}

int get\_kth\_number(int k) {

assert(1 <= k && k <= size());

return kth(root, k);

}

int order\_of\_key(const T& x) {

return order\_of\_key(root, x);

}

int size() {

return root->size;

}

};

## BST

class BST {

struct node {

int key;

node\* left, \* right, \* parent;

node() {

key = 0;

left = right = parent = NULL;

}

node(int key, node\* left = NULL, node\* right = NULL, node\* parent = NULL) :

key(key), left(left), right(right), parent(parent) {

}

};

typedef node\* nodeptr;

nodeptr minimum(nodeptr root) {

if (root->left == NULL)

return root;

return minimum(root->left);

}

nodeptr maximum(nodeptr root) {

if (root->right == NULL)

return root;

return maximum(root->right);

}

nodeptr successor(nodeptr cur) { //smallest key larger than cur

if (cur->right != NULL)

return minimum(cur->right);

nodeptr tmp = cur->parent;

while (tmp != NULL && tmp->right == cur)

cur = tmp, tmp = tmp->parent;

return tmp;

}

nodeptr bredecessor(nodeptr cur) { //biggest key less than cur

if (cur->left != NULL)

return maximum(cur->left);

nodeptr tmp = cur->parent;

while (tmp != NULL && tmp->left == cur)

cur = tmp, tmp = tmp->parent;

return tmp;

}

nodeptr find(nodeptr root, int key) {

if (root == NULL)

return NULL;

if (key == root->key)

return root;

if (key < root->key)

return find(root->left, key);

return find(root->right, key);

}

nodeptr insert(nodeptr root, int key) {

if (root == NULL)

root = new node(key);

else if (key < root->key) {

root->left = insert(root->left, key);

root->left->parent = root;

}

else if (key > root->key) {

root->right = insert(root->right, key);

root->right->parent = root;

}

return root;

}

nodeptr erase(nodeptr root, int key) {

if (root == NULL)

return root;

if (key < root->key) {

root->left = erase(root->left, key);

root->left->parent = root;

}

else if (key > root->key) {

root->right = erase(root->right, key);

root->right->parent = root;

}

else {

nodeptr tmp;

if (root->left == NULL || root->right == NULL) {

if (root->left == NULL)

tmp = root->right;

else

tmp = root->left;

free(root);

return tmp;

}

else {

tmp = successor(root);

root->key = tmp->key;

root->right = erase(root->right, tmp->key);

root->right->parent = root;

}

}

return root;

}

public:

nodeptr root;

BST() :

root(NULL) {

}

nodeptr find(int key) {

return find(root, key);

}

void insert(int key) {

root = insert(root, key);

}

void erase(int key) {

root = erase(root, key);

}

};

void inorder(nodeptr root) {

if (root == NULL)

return;

inorder(root->left);

cout << root->key << ' ';

inorder(root->right);

}

void preorder(nodeptr root) {

if (root == NULL)

return;

cout << root->key << ' ';

preorder(root->left);

preorder(root->right);

}

void postorder(nodeptr root) {

if (root == NULL)

return;

postorder(root->left);

postorder(root->right);

cout << root->key << ' ';

}

### AVL

struct AVLnode {

int key, height;

AVLnode\* left, \* right, \* parent;

static AVLnode\* sentinel;

AVLnode() {

parent = left = right = sentinel;

height = 0;

}

AVLnode(int key) : key(key) {

parent = left = right = sentinel;

height = 0;

}

void updateHeight() {

height = 1 + max(left->height, right->height);

}

int balanceFactor() {

return left->height - right->height;

}

};

AVLnode\* AVLnode::sentinel = new AVLnode();

class AVL : public BST {

typedef AVLnode\* nodeptr;

public:

nodeptr root;

AVL() : root(NULL) {}

void insert(int key) { root = insert(root, key); }

private:

nodeptr rightRotation(nodeptr Q) {

nodeptr P = Q->left;

Q->left = P->right;

Q->left->parent = Q;

P->right = Q;

P->parent = Q->parent;

Q->parent = P;

Q->updateHeight();

P->updateHeight();

return P;

}

nodeptr leftRotation(nodeptr P) {

nodeptr Q = P->right;

P->right = Q->left;

P->right->parent = P;

Q->left = P;

Q->parent = P->parent;

P->parent = Q;

Q->updateHeight();

P->updateHeight();

return Q;

}

nodeptr balance(nodeptr root) {

if (root->balanceFactor() == 2) {

if (root->left->balanceFactor() == -1)

root->left = leftRotation(root->left);

root = rightRotation(root);

}

else if (root->balanceFactor() == -2) {

if (root->right->balanceFactor() == 1)

root->right = rightRotation(root->right);

root = leftRotation(root);

}

return root;

}

nodeptr insert(nodeptr root, int key) {

if (root == AVLnode::sentinel)

return root = new AVLnode(key);

if (key < root->key) {

root->left = insert(root->left, key);

root->left->parent = root;

}

else if (key > root->key) {

root->right = insert(root->right, key);

root->right->parent = root;

}

root->updateHeight();

root = balance(root);

return root;

}

};

### Heap

template<class T, class cmp = less<T>>

class heap {

vector<T> v;

void check() const {

assert(size() > 0);

}

int parent(const int& node) const {

return (node == 0 ? -1 : (node - 1) / 2);

}

int right(const int& node) const {

int r = 2 \* node + 2;

return (r < size() ? r : -1);

}

int left(const int& node) const {

int l = 2 \* node + 1;

return (l < size() ? l : -1);

}

void reheapUp(const int& node) {

if (node == 0 || cmp()(v[parent(node)], v[node]))

return;

swap(v[node], v[parent(node)]);

reheapUp(parent(node));

}

void reheapDown(const int& node) {

int child = left(node);

if (child == -1)

return;

int rightChild = right(node);

if (rightChild != -1 && cmp()(v[rightChild], v[child]))

child = rightChild;

if (cmp()(v[node], v[child]))

return;

swap(v[node], v[child]);

reheapDown(child);

}

public:

int size() const {

return v.size();

}

void push(const int& val) {

v.push\_back(val);

reheapUp((int)v.size() - 1);

}

const T& top() const {

check();

return v[0];

}

void pop() {

check();

v[0] = v.back();

v.pop\_back();

reheapDown(0);

}

};

## Big Integer

class BigInt {

private:

#define CUR (\*this)

    const int BASE = 1000000000;//1e9

    vector<int> v;

public:

    BigInt() {

    }

    BigInt(const long long &val) {

        CUR = val;

    }

    BigInt(const string &val) {

        CUR = val;

    }

    int size() const {

        return v.size();

    }

    bool zero() const {

        return v.empty();

    }

    BigInt& operator =(long long val) {

        v.clear();

        while (val) {

            v.push\_back(val % BASE);

            val /= BASE;

        }

        return CUR;

    }

    BigInt& operator =(const BigInt &a) {

        v = a.v;

        return CUR;

    }

    BigInt& operator=(const string &s) {

        CUR = 0;

        for (const char &ch : s)

            CUR = CUR \* 10 + (ch - '0');

        return CUR;

    }

    /\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*compare\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*/

    bool operator <(const BigInt &a) const {

        if (a.size() != size())

            return size() < a.size();

        for (int i = size() - 1; i >= 0; i--) {

            if (v[i] != a.v[i])

                return v[i] < a.v[i];

        }

        return false;

    }

    bool operator >(const BigInt &a) const {

        return a < CUR;

    }

    bool operator ==(const BigInt &a) const {

        return (!(CUR < a) && !(a < CUR));

    }

    bool operator <=(const BigInt &a) const {

        return ((CUR < a) || !(a < CUR));

    }

    /\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*add\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*/

    BigInt operator +(const BigInt &a) const {

        BigInt res = CUR;

        int idx = 0, carry = 0;

        while (idx < a.size() || carry) {

            if (idx < a.size())

                carry += a.v[idx];

            if (idx == res.size())

                res.v.push\_back(0);

            res.v[idx] += carry;

            carry = res.v[idx] / BASE;

            res.v[idx] %= BASE;

            idx++;

        }

        return res;

    }

    BigInt& operator +=(const BigInt &a) {

        CUR = CUR + a;

        return CUR;

    }

    /\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*multiply\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*/

    BigInt operator \*(const BigInt &a) const {

        BigInt res;

        if (CUR.zero() || a.zero())

            return res;

        res.v.resize(size() + a.size());

        for (int i = 0; i < size(); i++) {

            if (v[i] == 0)

                continue;

            long long carry = 0;

            for (int j = 0; carry || j < a.size(); j++) {

                carry += 1LL \* v[i] \* (j < a.size() ? a.v[j] : 0);

                while (i + j >= res.size())

                    res.v.push\_back(0);

                carry += res.v[i + j];

                res.v[i + j] = carry % BASE;

                carry /= BASE;

            }

        }

        while (!res.v.empty() && res.v.back() == 0)

            res.v.pop\_back();

        return res;

    }

    BigInt& operator \*=(const BigInt &a) {

        CUR = CUR \* a;

        return CUR;

    }

    /\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*Division\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*/

    BigInt& operator /=(const int &a) {

        ll carry = 0;

        for (int i = (int) v.size() - 1; i >= 0; i--) {

            ll cur = v[i] + carry \* BASE;

            v[i] = cur / a;

            carry = cur % a;

        }

        while (!v.empty() && v.back() == 0)

            v.pop\_back();

        return CUR;

    }

    /\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*print\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*/

    friend ostream& operator<<(ostream &out, const BigInt &a) {

        out << (a.zero() ? 0 : a.v.back());

        for (int i = (int) a.v.size() - 2; i >= 0; i--)

            out << setfill('0') << setw(9) << a.v[i];

        return out;

    }

#undef CUR

};

# Graph

## Graph Data structures

### DSU

struct DSU {

vector<int> rank, parent, size;

vector<vector<int>> component;

int forsets;

DSU(int n) {

size = rank = parent = vector<int>(n + 1, 1);

component = vector<vector<int>>(n + 1);

forsets = n;

for (int i = 0; i <= n; i++) {

parent[i] = i;

component[i].push\_back(i);

}

}

int find\_set(int v) {

if (v == parent[v])

return v;

return parent[v] = find\_set(parent[v]);

}

void link(int par, int node) {

parent[node] = par;

size[par] += size[node];

for (const int& it : component[node])

component[par].push\_back(it);

component[node].clear();

if (rank[par] == rank[node])

rank[par]++;

forsets--;

}

bool union\_sets(int v, int u) {

v = find\_set(v), u = find\_set(u);

if (v != u) {

if (rank[v] < rank[u])

swap(v, u);

link(v, u);

}

return v != u;

}

bool same\_set(int v, int u) {

return find\_set(v) == find\_set(u);

}

int size\_set(int v) {

return size[find\_set(v)];

}

};

#### DSU apps

void Painting\_subarrays() {

struct Query {

int l, r, c;

Query(int l, int r, int c) :

l(l), r(r), c(c) {

}

};

int n, q;

cin >> n >> q;

DSU uf(n);

vector<int> ans(n + 1);

vector<Query> query(q);

for (int i = 0; i < q; i++)

cin >> query[i].l >> query[i].r >> query[i].c;

reverse(query.begin(), query.end());

for (auto q : query) {

int l = q.l, r = q.r, c = q.c;

for (int cur = uf.find\_set(l); cur <= r; cur = uf.find\_set(cur)) {

uf.parent[cur] = cur + 1;

ans[cur] = c;

}

}

}

void RMQ() {

struct Query {

int l, r, idx;

Query(int l, int r, int idx) :

l(l), r(r), idx(idx) {

}

};

int n, q;

cin >> n >> q;

vector<int> v(n);

vector < vector < Query >> query(n);

vector<int> ans(q);

DSU uf(n);

for (auto& a : v)

cin >> a;

for (int i = 0; i < q; i++) {

int l, r;

cin >> l >> r;

query[r].push\_back(Query(l, r, i));

}

stack<int> st;

for (int i = 0; i < n; i++) {

while (!st.empty() && v[st.top()] > v[i]) {

uf.parent[st.top()] = i;

st.pop();

}

st.push(i);

for (auto q : query[i])

ans[q.idx] = v[uf.find\_set(q.l)];

}

}

### DSU bipartiteness

struct DSU\_bipartiteness {

vector<int> bipartite, rank;

vector<pair<int, int>> parent;

DSU\_bipartiteness(int n) {

bipartite = rank = vector<int>(n + 1, 1);

parent = vector<pair<int, int>>(n + 1);

for (int i = 0; i <= n; i++)

parent[i] = { i, 0 };

}

pair<int, int> find\_set(int x) {

if (x == parent[x].first)

return parent[x];

int parity = parent[x].second;

parent[x] = find\_set(parent[x].first);

parent[x].second ^= parity;

return parent[x];

}

void union\_sets(int x, int y) {

pair<int, int> p = find\_set(x);

x = p.first;

int paX = p.second;

p = find\_set(y);

y = p.first;

int paY = p.second;

if (x == y) {

if (paX == paY)

bipartite[x] = false;

}

else {

if (rank[x] < rank[y])

swap(x, y);

parent[y] = { x, paX ^ paY ^ 1 };

bipartite[x] &= bipartite[y];

if (rank[x] == rank[y])

rank[x]++;

}

}

bool is\_bipartite(int x) {

return bipartite[find\_set(x).first];

}

};

### LCA

class LCA {

    int n, logN, root = 1;

    vector<int> depth;

    vector<vector<int>> adj, lca;

    void dfs(int node, int parent) {

        lca[node][0] = parent;

        depth[node] = (~parent ? depth[parent] + 1 : 0);

        for (int k = 1; k <= logN; k++) {

            int up\_parent = lca[node][k - 1];

            if (~up\_parent)

                lca[node][k] = lca[up\_parent][k - 1];

        }

        for (int child : adj[node])

            if (child != parent)

                dfs(child, node);

    }

public:

    LCA(const vector<vector<int>> &\_adj, int root = 1) :

            root(root), adj(\_adj) {

        adj = \_adj;

        n = adj.size() - 1;

        logN = log2(n);

        lca = vector<vector<int>>(n + 1, vector<int>(logN + 1, -1));

        depth = vector<int>(n + 1);

        dfs(root, -1);

    }

    int get\_LCA(int x, int y) {

        if (depth[x] < depth[y])

            swap(x, y);

        for (int k = logN; k >= 0; k--)

            if (depth[x] - (1 << k) >= depth[y])

                x = lca[x][k];

        if (x == y)

            return x;

        for (int k = logN; k >= 0; k--) {

            if (lca[x][k] != lca[y][k]) {

                x = lca[x][k], y = lca[y][k];

            }

        }

        return lca[x][0];

    }

    int get\_distance(int u, int v) {

        return depth[u] + depth[v] - 2 \* depth[get\_LCA(u, v)];

    }

    int shifting(int node, int dist) {

        for (int i = logN; i >= 0 && ~node; i--)

            if (dist & (1 << i))

                node = lca[node][i];

        return node;

    }

    edge get\_path(int u, int LCA) {

        edge rt;

        for (int k = logN; k >= 0; k--)

            if (depth[u] - (1 << k) >= depth[LCA]) {

                rt = merge(rt, lca[u][k]);

                u = lca[u][k].to;

            }

        return rt;

    }

};

### Heavy light decomposition

class heavy\_light\_decomposition { //1-based,if value in node,just update it after build chains

    int n, is\_value\_in\_edge;

    vector<int> parent, depth, heavy, root, pos\_in\_array, pos\_to\_node, size;

    const static int merge(int a, int b); //implement it

    struct array\_ds { //implement it

        int n;

        array\_ds(int n) :

                n(n) {

        }

        void update(int pos, int value);

        int query(int l, int r);

    } seg;

    struct TREE {

        int cnt\_edges = 1;

        vector<vector<int>> adj;

        //need for value in edges

        vector<vector<int>> edge\_idx;

        //edge\_to need for undirected tree //end of edge in directed tree

        vector<int> edge\_to, edge\_cost;

        TREE(int n) :

                adj(n + 1), edge\_idx(n + 1), edge\_to(n + 1), edge\_cost(n + 1) {

        }

        void add\_edge(int u, int v, int c) {

            adj[u].push\_back(v);

            adj[v].push\_back(u);

            edge\_idx[u].push\_back(cnt\_edges);

            edge\_idx[v].push\_back(cnt\_edges);

            edge\_cost[cnt\_edges] = c;

            cnt\_edges++;

        }

    } tree;

    int dfs\_hld(int node) {

        int size = 1, max\_sub\_tree = 0;

        for (int i = 0; i < (int) tree.adj[node].size(); i++) {

            int ch = tree.adj[node][i], edge\_idx = tree.edge\_idx[node][i];

            if (ch != parent[node]) {

                tree.edge\_to[edge\_idx] = ch;

                parent[ch] = node;

                depth[ch] = depth[node] + 1;

                int child\_size = dfs\_hld(ch);

                if (child\_size > max\_sub\_tree)

                    heavy[node] = ch, max\_sub\_tree = child\_size;

                size += child\_size;

            }

        }

        return size;

    }

    vector<tuple<int, int, bool>> get\_path(int u, int v) { //l,r,must\_reverse?

        vector<pair<int, int>> tmp[2];

        bool idx = 1;

        while (root[u] != root[v]) {

            if (depth[root[u]] > depth[root[v]]) {

                swap(u, v);

                idx = !idx;

            }

            //if value in edges ,you need value of root[v] also (connecter edge)

            tmp[idx].push\_back( { pos\_in\_array[root[v]], pos\_in\_array[v] });

            v = parent[root[v]];

        }

        if (depth[u] > depth[v]) {

            swap(u, v);

            idx = !idx;

        }

        if (!is\_value\_in\_edge || u != v)

            tmp[idx].push\_back( { pos\_in\_array[u] + is\_value\_in\_edge,

                    pos\_in\_array[v] });

        reverse(all(tmp[1]));

        vector<tuple<int, int, bool>> rt;

        for (int i = 0; i < 2; i++)

            for (auto &it : tmp[i])

                rt.emplace\_back(it.first, it.second, i == 0);

        return rt; //u is LCA

    }

public:

    heavy\_light\_decomposition(int n, bool is\_value\_in\_edge) :

            n(n), is\_value\_in\_edge(is\_value\_in\_edge), seg(n + 1), tree(n + 1) {

        heavy = vector<int>(n + 1, -1);

        parent = depth = root = pos\_in\_array = pos\_to\_node = size = vector<int>(

                n + 1);

    }

    void add\_edge(int u, int v, int c = 0) {

        tree.add\_edge(u, v, c);

    }

    void build\_chains(int src = 1) {

        parent[src] = -1;

        dfs\_hld(src);

        for (int chain\_root = 1, pos = 1; chain\_root <= n; chain\_root++) {

            if (parent[chain\_root] == -1

                    || heavy[parent[chain\_root]] != chain\_root)

                for (int j = chain\_root; j != -1; j = heavy[j]) {

                    root[j] = chain\_root;

                    pos\_in\_array[j] = pos++;

                    pos\_to\_node[pos\_in\_array[j]] = j;

                }

        }

        if (is\_value\_in\_edge)

            for (int i = 1; i < n; i++)

                update\_edge(i, tree.edge\_cost[i]);

    }

    void update\_node(int node, int value) {

        seg.update(pos\_in\_array[node], value);

    }

    void update\_edge(int edge\_idx, int value) {

        update\_node(tree.edge\_to[edge\_idx], value);

    }

    void update\_path(int u, int v, ll c) {

        vector<tuple<int, int, bool>> intervals = get\_path(u, v);

        for (auto &it : intervals)

            seg.update(get<0>(it), get<1>(it), c);

    }

    node query\_in\_path(int u, int v) {

        vector<tuple<int, int, bool>> intervals = get\_path(u, v);

        //initial value,check if handling u == v

        node query\_res = 0;

        for (auto &it : intervals) {

            int l, r;

            bool rev;

            tie(l, r, rev) = it;

            node cur = seg.query(l, r);

            if (rev)

                cur.reverse();

            query\_res = node(query\_res, cur);

        }

        return query\_res;

    }

};

### centroid decomposition

class centroid\_decomposition {

    vector<bool> centroidMarked;

    vector<int> size;

    void dfsSize(int node, int par) {

        size[node] = 1;

        for (int ch : adj[node])

            if (ch != par && !centroidMarked[ch]) {

                dfsSize(ch, node);

                size[node] += size[ch];

            }

    }

    int getCenter(int node, int par, int size\_of\_tree) {

        bool is\_centroid = true;

        int heaviest\_child = -1;

        for (int ch : adj[node])

            if (ch != par && !centroidMarked[ch]) {

                if (size[ch] > size\_of\_tree / 2)

                    is\_centroid = false;

                if (heaviest\_child == -1 || size[ch] > size[heaviest\_child])

                    heaviest\_child = ch;

            }

        if (is\_centroid && size\_of\_tree - size[node] <= size\_of\_tree / 2)

            return node;

        assert(heaviest\_child != -1);

        return getCenter(heaviest\_child, node, size\_of\_tree);

    }

    int getCentroid(int src) {

        dfsSize(src, -1);

        int centroid = getCenter(src, -1, size[src]);

        centroidMarked[centroid] = true; //need to mark it after solve?

        return centroid;

    }

    int decomposeTree(int root) {

        root = getCentroid(root);

        solve(root);

        for (int ch : adj[root]) {

            if (centroidMarked[ch])

                continue;

            int centroid\_of\_subtree = decomposeTree(ch);

            //note: root and centroid\_of\_subtree probably not have a direct edge in adj

            centroidTree[root].push\_back(centroid\_of\_subtree);

            centroidParent[centroid\_of\_subtree] = root;

        }

        return root;

    }

    void calc(int node, int par) {

        //TO-DO

        for (int ch : adj[node])

            if (ch != par && !centroidMarked[ch])

                calc(ch, node);

    }

    void add(int node, int par) {

        //TO-DO

        for (int ch : adj[node])

            if (ch != par && !centroidMarked[ch])

                add(ch, node);

    }

    void remove(int node, int par) {

        //TO-DO

        for (int ch : adj[node])

            if (ch != par && !centroidMarked[ch])

                remove(ch, node);

    }

    void solve(int root) {

        //add root

        for (int ch : adj[root])

            if (!centroidMarked[ch]) {

                calc(ch, root);

                add(ch, root);

            }

        //remove root

        for (int ch : adj[root])

            if (!centroidMarked[ch])

                remove(ch, root);

    }

public:

    int n, root;

    vector<vector<int>> adj, centroidTree;

    vector<int> centroidParent;

    centroid\_decomposition(vector<vector<int>> &adj) :

            adj(adj) {

        n = (int) adj.size() - 1;

        size = vector<int>(n + 1);

        centroidTree = vector<vector<int>>(n + 1);

        centroidParent = vector<int>(n + 1, -1);

        centroidMarked = vector<bool>(n + 1);

        root = decomposeTree(1);

    }

};

## shortest path algorithms

### Dijkstra

struct edge {

int from, to, weight;

edge() {

from = to = weight = 0;

}

edge(int from, int to, int weight) :

from(from), to(to), weight(weight) {

}

bool operator <(const edge& other) const {

return weight > other.weight;

}

};

vector<vector<edge>> adj;

//O(E\*log(v))

void dijkstra(int src, int dest = -1) {

priority\_queue<edge> q;

vector<int> dis(adj.size(), INT\_MAX), prev(adj.size(), -1);

q.push(edge(-1, src, 0));

dis[src] = 0;

while (!q.empty()) {

edge e = q.top();

q.pop();

if (e.weight > dis[e.to])

continue;

prev[e.to] = e.from;

if (e.to == dest)

break;

for (edge ne : adj[e.to])

if (dis[ne.to] > dis[e.to] + ne.weight) {

ne.weight = dis[ne.to] = dis[e.to] + ne.weight;

q.push(ne);

}

}

vector<int> path;

while (dest != -1) {

path.push\_back(dest);

dest = prev[dest];

}

reverse(path.begin(), path.end());

}

### Bellmanford

vector<edge> edgeList;

//O(V\*E)

void bellmanford(int n, int src, int dest = -1) {

vector<int> dis(n + 1, oo), prev(n + 1, -1);

dis[src] = 0;

bool negativeCycle = false;

int last = -1, tmp = n;

while (tmp--) {

last = -1;

for (edge e : edgeList)

if (dis[e.to] > dis[e.from] + e.weight) {

dis[e.to] = dis[e.from] + e.weight;

prev[e.to] = e.from;

last = e.to;

}

if (last == -1)

break;

if (tmp == 0)

negativeCycle = true;

}

if (last != -1) {

for (int i = 0; i < n; i++)

last = prev[last];

vector<int> cycle;

for (int cur = last; cur != last || cycle.size() > 1; cur = prev[cur])

cycle.push\_back(cur);

reverse(cycle.begin(), cycle.end());

}

vector<int> path;

while (dest != -1) {

path.push\_back(dest);

dest = prev[dest];

}

reverse(path.begin(), path.end());

}

#### Difference constraints

void difference\_constraints() {

int m;

cin >> m;

int cnt = 1;

while (m--) {

string x1, x2;

int w; // x1 - x2 <= w

cin >> x1 >> x2 >> w;

map<string, int> id;

if (id.find(x1) == id.end())

id[x1] = cnt++;

if (id.find(x2) == id.end())

id[x2] = cnt++;

edgeList.emplace\_back(id[x2], id[x1], w);

}

for (int i = 1; i < cnt; i++)

edgeList.emplace\_back(cnt, i, 0);

bellmanford(cnt, cnt);

}

### Floyed

vector<vector<int>> adj, par;

// adj[i][j] = oo , adj[i][i] = 0 , par[i][j] = i

void init(int n) {

par = adj = vector<vector<int>>(n + 1, vector<int>(n + 1, oo));

for (int i = 1; i <= n; i++)

adj[i][i] = 0;

for (int i = 1; i <= n; i++)

for (int j = 1; j <= n; j++)

par[i][j] = i;

}

void floyd() {

for (int k = 1; k < adj.size(); k++)

for (int i = 1; i < adj.size(); i++)

for (int j = 1; j < adj.size(); j++)

if (adj[i][j] > adj[i][k] + adj[k][j]) {

adj[i][j] = adj[i][k] + adj[k][j];

par[i][j] = par[k][j];

}

}

void buildPath(int src, int dest) {

vector<int> path;

while (src != dest) {

path.push\_back(dest);

dest = par[src][dest];

}

path.push\_back(src);

reverse(path.begin(), path.end());

}

### SPFA

vector<vector<edge>> adj;

void spfa(int src) {

    enum visit {

        finished, in\_queue, not\_visited

    };

    int n = adj.size();

    vector<int> dis(n, INF), prev(n, -1), state(n, not\_visited);

    dis[src] = 0;

    deque<int> q;

    q.push\_back(src);

    while (!q.empty()) {

        int u = q.front();

        q.pop\_front();

        state[u] = finished;

        for (auto &e : adj[u]) {

            if (dis[e.to] > dis[e.from] + e.cost) {

                dis[e.to] = dis[e.from] + e.cost;

                prev[e.to] = e.from;

                if (state[e.to] == not\_visited)

                    q.push\_back(e.to);

                else if (state[e.to] == finished)

                    q.push\_front(e.to);

                state[e.to] = in\_queue;

            }

        }

    }

}

## MST

### Kruskal

struct edge {

int from, to;

ll weight;

edge() {

from = to = weight = 0;

}

edge(int from, int to, ll weight) :

from(from), to(to), weight(weight) {

}

bool operator <(const edge& other) const {

return weight < other.weight;

}

};

vector<edge> edgeList;

pair<int, vector<edge>> MST\_Kruskal(int n) {//O(edges\*log(edges))

DSU uf(n);

vector < edge > edges;

int mstCost = 0;

sort(edgeList.begin(), edgeList.end());

for (auto e : edgeList)

if (uf.union\_sets(e.from, e.to)) {

mstCost += e.weight;

edges.push\_back(e);

}

if (edges.size() != n - 1)

return { INT\_MAX,vector<edge>() };

return { mstCost,edges };

}

int miniMax(int src, int dest, int n) {

int max = INT\_MIN;

DSU uf(n);

sort(edgeList.begin(), edgeList.end());

for (auto e : edgeList) {

if (uf.same\_set(src, dest))

return max;

uf.union\_sets(e.from, e.to);

max = e.weight;

}

return max;

}

//O(edges\*log(edges) + nodes\*nodes)

pair<int, vector<edge>> SMST\_Kruskal(int n) {

DSU uf(n);

sort(edgeList.begin(), edgeList.end());

vector<edge> take, leave;

int mstCost = 0;

for (auto e : edgeList)

if (uf.union\_sets(e.from, e.to)) {

mstCost += e.weight;

take.push\_back(e);

}

else leave.push\_back(e);

pair<int, vector<edge>> ret = { INT\_MAX, vector<edge>() };

for (int i = 0; i < take.size(); i++) {

uf = DSU(n);

vector < edge > edges;

mstCost = 0;

for (int j = 0; j < take.size(); j++) {

if (i == j)

continue;

uf.union\_sets(take[j].from, take[j].to);

mstCost += take[j].weight;

edges.push\_back(take[j]);

}

for (edge e : leave) {

if (uf.union\_sets(e.from, e.to)) {

mstCost += e.weight;

edges.push\_back(e);

break;

}

}

if (edges.size() == n - 1 && ret.first < mstCost)

ret = { mstCost, edges };

}

return ret;

}

### Prim

struct edge {

int from, to, weight;

edge() {

from = to = weight = 0;

}

edge(int from, int to, int weight) :

from(from), to(to), weight(weight) {

}

bool operator <(const edge& other) const {

return weight > other.weight;

}

};

vector<vector<edge>> adj;

vector<edge> prim(int node) {

vector<bool> vis(adj.size());

priority\_queue<edge> q;

vector<edge> edges;

q.push(edge(-1, node, 0));

while (!q.empty()) {

edge e = q.top();

q.pop();

if (vis[e.to])

continue;

vis[e.to] = true;

if (e.from != -1)

edges.push\_back(e);

for (edge ch : adj[e.to])

if (!vis[ch.to])

q.push(ch);

}

return edges;//check it connected or not

}

### SMST

struct edge {

int from, to;

ll weight;

edge() {

from = to = weight = 0;

}

edge(int from, int to, ll weight) :

from(from), to(to), weight(weight) {

}

bool operator <(const edge& other) const {

return weight < other.weight;

}

};

int MST\_Kruskal(int n, vector<edge> edgeList, vector<edge>& take,

vector<edge>& leave) {

DSU uf(n);

vector<edge> edges;

sort(edgeList.begin(), edgeList.end());

int mst\_cost = 0;

for (auto e : edgeList)

if (uf.union\_sets(e.from, e.to)) {

take.push\_back(e);

mst\_cost += e.weight;

}

else leave.push\_back(e);

return mst\_cost;

}

struct LCA {

#define INIT { -1, -2 }

struct data {

int lca = -1;

pair<int, int> max\_edges = INIT; //first max,second max (distinct)

};

pair<int, int> merge(pair<int, int> a, pair<int, int> b) {

if (a.first < b.first)

swap(a, b);

if (b.first == a.first)

a.second = max(a.second, b.second);

else if (b.first > a.second)

a.second = b.first;

return a;

}

int logN;

vector<vector<data>> lca;

vector<vector<edge>> adj;

vector<int> depth;

void dfs(int node, int par) {

for (edge e : adj[node])

if (e.to != par) {

depth[e.to] = depth[node] + 1;

lca[e.to][0].max\_edges.first = e.weight;

lca[e.to][0].lca = node;

dfs(e.to, node);

}

}

LCA(int n, vector<edge>& edges) :

adj(n + 1) {

for (auto& e : edges) {

adj[e.from].push\_back(e);

adj[e.to].push\_back(edge(e.to, e.from, e.weight));

}

logN = log2(n);

depth = vector<int>(n + 1);

lca = vector<vector<data>>(n + 1, vector<data>(logN + 1));

dfs(1, -1);

for (int k = 1; k <= logN; k++)

for (int node = 1; node <= n; node++) {

int par = lca[node][k - 1].lca;

if (~par) {

lca[node][k].lca = lca[par][k - 1].lca;

lca[node][k].max\_edges = merge(lca[node][k - 1].max\_edges,

lca[par][k - 1].max\_edges);

}

}

}

pair<int, int> max\_two\_edges(int u, int v) {

pair<int, int> ans = INIT;

if (depth[u] < depth[v])

swap(u, v);

for (int i = logN; i >= 0; i--)

if (depth[u] - (1 << i) >= depth[v]) {

ans = merge(ans, lca[u][i].max\_edges);

u = lca[u][i].lca;

}

if (u == v)

return ans;

for (int i = logN; i >= 0; i--)

if (lca[u][i].lca != lca[v][i].lca) {

ans = merge(ans, lca[u][i].max\_edges);

ans = merge(ans, lca[v][i].max\_edges);

u = lca[u][i].lca;

v = lca[v][i].lca;

}

ans = merge(ans, lca[u][0].max\_edges);

ans = merge(ans, lca[v][0].max\_edges);

return ans;

}

};

int main() {

run();

int t;

cin >> t;

for (int I = 1; I <= t; I++) {

int n, e;

cin >> n >> e;

vector<edge> edgeList(e);

for (auto& it : edgeList)

cin >> it.from >> it.to >> it.weight;

vector<edge> take, leave;

int mst\_cost = MST\_Kruskal(n, edgeList, take, leave);

if (take.size() != n - 1) {

cout << "No way\n";

continue;

}

LCA tree(n, take);

ll rt = INF;

for (edge e : leave) {

pair<int, int> p = tree.max\_two\_edges(e.from, e.to);

rt = min(rt, mst\_cost - p.first + e.weight);

}

if (rt == INF)

cout << "No second way\n";

else

cout << rt << endl;

}

}

## Tarjan

### SCC

vector<vector<int>> adj, scc;

vector<set<int>> dag;

vector<int> dfs\_num, dfs\_low, compId;

vector<bool> inStack;

stack<int> stk;

int timer;

void dfs(int node) {

dfs\_num[node] = dfs\_low[node] = ++timer;

stk.push(node);

inStack[node] = 1;

for (int child : adj[node])

if (!dfs\_num[child]) {

dfs(child);

dfs\_low[node] = min(dfs\_low[node], dfs\_low[child]);

}

else if (inStack[child])

dfs\_low[node] = min(dfs\_low[node], dfs\_num[child]);

//can be dfs\_low[node] = min(dfs\_low[node], dfs\_low[child]);

if (dfs\_low[node] == dfs\_num[node]) {

scc.push\_back(vector<int>());

int v = -1;

while (v != node) {

v = stk.top();

stk.pop();

inStack[v] = 0;

scc.back().push\_back(v);

compId[v] = scc.size() - 1;

}

}

}

void SCC() {

timer = 0;

dfs\_num = dfs\_low = compId = vector<int>(adj.size());

inStack = vector<bool>(adj.size());

scc = vector<vector<int>>();

for (int i = 1; i < adj.size(); i++)

if (!dfs\_num[i])

dfs(i);

}

void DAG() {

dag = vector<set<int>>(scc.size());

for (int i = 1; i < adj.size(); i++)

for (int j : adj[i])

if (compId[i] != compId[j])

dag[compId[i]].insert(compId[j]);

}

### Articulation points and bridges

vector<vector<int>> adj;

vector<int> dfs\_num, dfs\_low;

vector<bool> articulation\_point;

vector<pair<int, int>> bridge;

stack<pair<int, int>> edges;

vector<vector<pair<int, int>>> BCC; //biconnected components

int timer, cntChild;

void dfs(int node, int par) {

dfs\_num[node] = dfs\_low[node] = ++timer;

for (int child : adj[node]) {

if (par != child && dfs\_num[child] < dfs\_num[node])

edges.push({ node, child });

if (!dfs\_num[child]) {

if (par == -1)

cntChild++;

dfs(child, node);

if (dfs\_low[child] >= dfs\_num[node]) {

articulation\_point[node] = 1;

//get biconnected component

BCC.push\_back(vector<pair<int, int>>());

pair<int, int> edge;

do {

edge = edges.top();

BCC.back().push\_back(edge);

edges.pop();

} while (edge.first != node || edge.second != child);

}

if (dfs\_low[child] > dfs\_num[node]) //can be (dfs\_low[child] == dfs\_num[child])

bridge.push\_back({ node, child });

dfs\_low[node] = min(dfs\_low[node], dfs\_low[child]);

}

else if (child != par)

dfs\_low[node] = min(dfs\_low[node], dfs\_num[child]);

}

}

void articulation\_points\_and\_bridges() {

timer = 0;

dfs\_num = dfs\_low = vector<int>(adj.size());

articulation\_point = vector<bool>(adj.size());

bridge = vector<pair<int, int>>();

for (int i = 1; i < adj.size(); i++)

if (!dfs\_num[i]) {

cntChild = 0;

dfs(i, -1);

articulation\_point[i] = cntChild > 1;

}

}

## Edge classification

vector<vector<int>> adj;

vector<int> start, finish;

int timer;

void dfsEdgeClassification(int node) {

start[node] = timer++;

for (int child : adj[node]) {

if (start[child] == -1)

dfsEdgeClassification(child);

else {

if (finish[child] == -1)

; // Back Edge

else if (start[node] < start[child])

; // Forward Edge

else; // Cross Edge

}

}

finish[node] = timer++;

}

## 2-SAT

#include"..\strongly\_connected\_component.h"

int n;

int Not(int x) {

return (x > n ? x - n : x + n);

}

void addEdge(int a, int b) {

adj[Not(a)].push\_back(b);

adj[Not(b)].push\_back(a);

}

void add\_xor\_edge(int a, int b) {

addEdge(Not(a), Not(b));

addEdge(a, b);

}

bool \_2SAT(vector<int>& value) {

SCC();

for (int i = 1; i <= n; i++)

if (compId[i] == compId[Not(i)])

return false;

vector<int> assign(scc.size(), -1);

for (int i = 0; i < scc.size(); i++)

if (assign[i] == -1) {

assign[i] = true;

assign[compId[Not(scc[i].back())]] = false;

}

for (int i = 1; i <= n; i++)

value[i] = assign[compId[i]];

return true;

}

## Flows

### Maximum bipartite matching

vector<vector<int>> adj;

vector<int> rowAssign, colAssign, vis;

int test\_id;

bool canMatch(int i) {

for (int j : adj[i]) {

if (vis[j] == test\_id)

continue;

vis[j] = test\_id;

if (colAssign[j] == -1 || canMatch(colAssign[j])) {

colAssign[j] = i;

rowAssign[i] = j;

return true;

}

}

return false;

}

// O(rows \* edges) //number of operation could by strictly less than order (1e5\*1e5->AC)

int maximum\_bipartite\_matching(int rows, int cols) {

int maxFlow = 0;

rowAssign = vector<int>(rows, -1);

colAssign = vector<int>(cols, -1);

vis = vector<int>(cols);

for (int i = 0; i < rows; i++) {

test\_id++;

if (canMatch(i))

maxFlow++;

}

vector<pair<int, int>> matches;

for (int j = 0; j < cols; j++)

if (~colAssign[j])

matches.push\_back({ colAssign[j], j });

return maxFlow;

}

### Edmonds Karp

//O( V \* E \* E)

#define INF 0x3f3f3f3f3f3f3f3fLL

int n;

int capacity[101][101];

int getPath(int src, int dest, vector<int> &parent) {

    parent = vector<int>(n + 1, -1);

    queue<pair<int, int>> q;

    q.push( { src, INF });

    while (q.size()) {

        int cur = q.front().first, flow = q.front().second;

        q.pop();

        if (cur == dest)

            return flow;

        for (int i = 1; i <= n; i++)

            if (parent[i] == -1 && capacity[cur][i]) {

                parent[i] = cur;

                q.push( { i, min(flow, capacity[cur][i]) });

                if (i == dest)  return q.back().second;

            }

    }

    return 0;

}

int Edmonds\_Karp(int source, int sink) {

    int max\_flow = 0;

    int new\_flow = 0;

    vector<int> parent(n + 1, -1);

    while (new\_flow = getPath(source, sink, parent)) {

        max\_flow += new\_flow;

        int cur = sink;

        while (cur != source) {

            int prev = parent[cur];

            capacity[prev][cur] -= new\_flow;

            capacity[cur][prev] += new\_flow;

            cur = prev;

        };

    }

    return max\_flow;

}

### Dinic

//O(V\*V\*E) more faster

struct Dinic { //0-based

    struct flowEdge {

        int from, to;

        ll cap, flow = 0;

        flowEdge(int from, int to, ll cap) :

                from(from), to(to), cap(cap) {

        }

    };

    vector<flowEdge> edges;

    int n, m = 0, source, sink;

    vector<vector<int>> adj;

    vector<int> level, ptr;

    Dinic(int n, int source, int sink) :

            n(n), source(source), sink(sink), adj(n), level(n), ptr(n) {

    }

    void addEdge(int u, int v, ll cap) {

        edges.emplace\_back(u, v, cap);

        edges.emplace\_back(v, u, 0);

        adj[u].push\_back(m);

        adj[v].push\_back(m + 1);

        m += 2;

    }

    bool bfs() {

        queue<int> q;

        level = vector<int>(n, -1);

        level[source] = 0;

        q.push(source);

        while (!q.empty()) {

            int cur = q.front();

            q.pop();

            for (auto &id : adj[cur]) {

                if (edges[id].cap - edges[id].flow <= 0)

                    continue;

                int nxt = edges[id].to;

                if (level[nxt] != -1)

                    continue;

                level[nxt] = level[cur] + 1;

                q.push(nxt);

            }

        }

        return level[sink] != -1;

    }

    ll dfs(int node, ll cur\_flow) {

        if (cur\_flow == 0 || node == sink)

            return cur\_flow;

        for (int &cid = ptr[node]; cid < adj[node].size(); cid++) {

            int id = adj[node][cid];

            int nxt = edges[id].to;

            if (level[node] + 1 != level[nxt]

                    || edges[id].cap - edges[id].flow <= 0)

                continue;

            ll tmp = dfs(nxt, min(cur\_flow, edges[id].cap - edges[id].flow));

            if (tmp == 0)

                continue;

            edges[id].flow += tmp;

            edges[id ^ 1].flow -= tmp;

            return tmp;

        }

        return 0;

    }

    ll flow() {

        ll max\_flow = 0;

        while (bfs()) {

            fill(ptr.begin(), ptr.end(), 0);

            while (ll pushed = dfs(source, INF))

                max\_flow += pushed;

        }

        return max\_flow;

    }

};

### Min cost Max flow

struct MCMF { //0-based

    struct edge {

        int from, to, cost, cap, flow, backEdge;

        edge() {

            from = to = cost = cap = flow = backEdge = 0;

        }

        edge(int from, int to, int cost, int cap, int flow, int backEdge) :

                from(from), to(to), cost(cost), cap(cap), flow(flow), backEdge(

                        backEdge) {

        }

        bool operator <(const edge &other) const {

            return cost < other.cost;

        }

    };

    int n, src, dest;

    vector<vector<edge>> adj;

    const int OO = 1e9;

    MCMF(int n, int src, int dest) :

            n(n), src(src), dest(dest), adj(n) {

    }

    void addEdge(int u, int v, int cost, int cap) {

        edge e1 = edge(u, v, cost, cap, 0, adj[v].size());

        edge e2 = edge(v, u, -cost, 0, 0, adj[u].size());

        adj[u].push\_back(e1);

        adj[v].push\_back(e2);

    }

    pair<int, int> minCostMaxFlow() {

        int maxFlow = 0, cost = 0;

        while (true) {

            vector<pair<int, int>> path = spfa();

            if (path.empty())

                break;

            int new\_flow = OO;

            for (auto &it : path) {

                edge &e = adj[it.first][it.second];

                new\_flow = min(new\_flow, e.cap - e.flow);

            }

            for (auto &it : path) {

                edge &e = adj[it.first][it.second];

                e.flow += new\_flow;

                cost += new\_flow \* e.cost;

                adj[e.to][e.backEdge].flow -= new\_flow;

            }

            maxFlow += new\_flow;

        }

        return {maxFlow,cost};

    }

    enum visit {

        finished, in\_queue, not\_visited

    };

    vector<pair<int, int>> spfa() {

        vector<int> dis(n, OO), prev(n, -1), from\_edge(n), state(n,

                not\_visited);

        deque<int> q;

        dis[src] = 0;

        q.push\_back(src);

        while (!q.empty()) {

            int u = q.front();

            q.pop\_front();

            state[u] = finished;

            for (int i = 0; i < adj[u].size(); i++) {

                edge e = adj[u][i];

                if (e.flow >= e.cap || dis[e.to] <= dis[u] + e.cost)

                    continue;

                dis[e.to] = dis[u] + e.cost;

                prev[e.to] = u;

                from\_edge[e.to] = i;

                if (state[e.to] == in\_queue)

                    continue;

                if (state[e.to] == finished

                        || (!q.empty() && dis[q.front()] > dis[e.to]))

                    q.push\_front(e.to);

                else

                    q.push\_back(e.to);

                state[e.to] = in\_queue;

            }

        }

        if (dis[dest] == OO)

            return {};

        vector<pair<int, int>> path;

        int cur = dest;

        while (cur != src) {

            path.push\_back( { prev[cur], from\_edge[cur] });

            cur = prev[cur];

        }

        reverse(path.begin(), path.end());

        return path;

    }

};

# String

## Hashing

struct hashing {

int MOD, BASE;

vector<int> Hash, modInv;

hashing(string s, int MOD, int BASE, char first\_char = 'a') :

MOD(MOD), BASE(BASE), Hash(sz(s) + 1), modInv(sz(s) + 1) {

modInv[0] = 1;

ll base = 1;

for (int i = 1; i <= sz(s); i++) {

Hash[i] = (Hash[i - 1] + (s[i - 1] - first\_char + 1) \* base) % MOD;

modInv[i] = power(base, MOD - 2, MOD);

base = (base \* BASE) % MOD;

}

}

int getHash(int l, int r) { //1-based

return ((Hash[r] - Hash[l - 1] + MOD) % MOD \* modInv[l]) % MOD;

}

};

//MOD = 1e9 + 9 ,BASE = 31

//MOD = 2000000011 ,BASE = 53 ->careful of overflow

//\*\*\*\*\*\*\*\*\*\*\*\*\*

//MOD = 998634293,BASE = 953

//MOD = 986464091,BASE = 1013

## KMP

string pattern;

vector<int> longestPrefix;

int fail(int k, char nxt) {

while (k > 0 && pattern[k] != nxt)

k = longestPrefix[k - 1];

if (nxt == pattern[k])

k++;

return k;

}

void failure\_function() {

int n = pattern.size();

longestPrefix = vector<int>(n);

for (int i = 1, k = 0; i < n; i++)

longestPrefix[i] = k = fail(k, pattern[i]);

}

void KMP(const string& str) {

int n = str.size();

int m = pattern.size();

for (int i = 0, k = 0; i < n; i++) {

k = fail(k, str[i]);

if (k == m) {

cout << i - m + 1 << endl; //0-based

k = longestPrefix[k - 1]; // if you want next match

}

}

}

## Trie tree

class trie {

    struct trie\_node {

        bool is\_leaf = false;

        map<char, int> next;

        bool have\_next(char ch) {

            return next.find(ch) != next.end();

        }

        int& operator[](char ch) {

            return next[ch];

        }

    };

    vector<trie\_node> t;

public:

    trie() {

        t.push\_back(trie\_node());

    }

    void insert(const string &s) {

        int root = 0;

        for (const char &ch : s) {

            if (!t[root].have\_next(ch)) {

                t.push\_back(trie\_node());

                t[root][ch] = t.size() - 1;

                //t[root][ch] = add\_node();doesn't work if next is array

            }

            root = t[root][ch];

        }

        t[root].is\_leaf = true;

    }

    bool find(const string &s) {

        int root = 0;

        for (const char &ch : s) {

            if (!t[root].have\_next(ch))

                return false;

            root = t[root][ch];

        }

        return t[root].is\_leaf;

    }

};

## Aho Corasick

struct aho\_corasick {

    struct trie\_node {

        vector<int> pIdxs; //probably take memory limit

        map<char, int> next;

        int fail;

        trie\_node() :

                fail(-1) {

        }

        bool have\_next(char ch) {

            return next.find(ch) != next.end();

        }

        int& operator[](char ch) {

            return next[ch];

        }

    };

    vector<trie\_node> t;

    vector<string> patterns;

    vector<int> end\_of\_pattern;

    vector<vector<int>> adj;

    int insert(const string &s, int patternIdx) {

        int root = 0;

        for (const char &ch : s) {

            if (!t[root].have\_next(ch)) {

                t.push\_back(trie\_node());

                t[root][ch] = t.size() - 1;

            }

            root = t[root][ch];

        }

        t[root].pIdxs.push\_back(patternIdx);

        return root;

    }

    int next\_state(int cur, char ch) {

        while (cur > 0 && !t[cur].have\_next(ch))

            cur = t[cur].fail;

        if (t[cur].have\_next(ch))

            return t[cur][ch];

        return 0;

    }

    void buildAhoTree() {

        queue<int> q;

        for (auto &child : t[0].next) {

            q.push(child.second);

            t[child.second].fail = 0;

        }

        while (!q.empty()) {

            int cur = q.front();

            q.pop();

            for (auto &child : t[cur].next) {

                int k = next\_state(t[cur].fail, child.first);

                t[child.second].fail = k;

                vector<int> &idxs = t[child.second].pIdxs;

                //dp[child.second] = max(dp[child.second],dp[k]);

                idxs.insert(idxs.end(), all(t[k].pIdxs));

                q.push(child.second);

            }

        }

    }

    void buildFailureTree() {

        adj = vector<vector<int>>(t.size());

        for (int i = 1; i < t.size(); i++)

            adj[t[i].fail].push\_back(i);

    }

    aho\_corasick(const vector<string> &\_patterns) {

        t.push\_back(trie\_node());

        patterns = \_patterns;

        end\_of\_pattern = vector<int>(patterns.size());

        for (int i = 0; i < patterns.size(); i++)

            end\_of\_pattern[i] = insert(patterns[i], i);

        buildAhoTree();

        buildFailureTree();

    }

    vector<vector<int>> match(const string &str) {

        int k = 0;

        vector<vector<int>> rt(patterns.size());

        for (int i = 0; i < str.size(); i++) {

            k = next\_state(k, str[i]);

            for (auto &it : t[k].pIdxs)

                rt[it].push\_back(i);

        }

        return rt;

    }

};

## Suffix Automaton

struct suffix\_automaton {

    struct state {

        int len, link = 0, cnt = 0;

        bool terminal = false, is\_clone = false;

        map<char, int> next;

        state(int len = 0) :

                len(len) {

        }

        bool have\_next(char ch) {

            return next.find(ch) != next.end();

        }

        void clone(const state &other, int nlen) {

            len = nlen;

            next = other.next;

            link = other.link;

            is\_clone = true;

        }

    };

    vector<state> st;

    int last = 0;

    suffix\_automaton() {

        st.push\_back(state());

        st[0].link = -1;

    }

    suffix\_automaton(const string &s) :

            suffix\_automaton() {

        for (char ch : s)

            extend(ch);

        mark\_terminals();

    }

    void mark\_terminals() {

        for (int cur = last; cur > 0; cur = st[cur].link)

            st[cur].terminal = true;

    }

    void extend(char c) {

        int cur = st.size();

        st.push\_back(state(st[last].len + 1));

        st[cur].cnt = 1;

        int p = last;

        last = cur;

        while (p != -1 && !st[p].have\_next(c)) {

            st[p].next[c] = cur;

            p = st[p].link;

        }

        if (p == -1)

            return;

        int q = st[p].next[c];

        if (st[p].len + 1 == st[q].len) {

            st[cur].link = q;

            return;

        }

        int clone = st.size();

        st.push\_back(state());

        st[clone].clone(st[q], st[p].len + 1);

        while (p != -1 && st[p].next[c] == q) {

            st[p].next[c] = clone;

            p = st[p].link;

        }

        st[q].link = st[cur].link = clone;

    }

    void calc\_number\_of\_occurrences() {

        vector<vector<int>> lvl(st[last].len + 1);

        for (int i = 1; i < st.size(); i++)

            lvl[st[i].len].push\_back(i);

        for (int i = st[last].len; i >= 0; i--)

            for (auto cur : lvl[i])

                st[st[cur].link].cnt += st[cur].cnt;

    }

    vector<ll> dp;

    ll Count(int cur) { //count number of paths

        ll &rt = dp[cur];

        if (rt)

            return rt;

        rt = 1;

        for (auto ch : st[cur].next)

            rt += Count(ch.second);

        return rt;

    }

    string kth\_substring(ll k) { //1-based,different substring,0 = ""

        assert(k <= Count(0));

        string rt;

        int cur = 0;

        while (k > 0) {

            for (auto ch : st[cur].next) {

                if (Count(ch.second) < k)

                    k -= Count(ch.second);

                else {

                    rt += ch.first;

                    cur = ch.second;

                    k--;

                    break;

                }

            }

        }

        return rt;

    }

    string longest\_common\_substring(const string &t) {

        int cur = 0, l = 0, mx = 0, idx = 0;

        for (int i = 0; i < t.size(); i++) {

            while (cur > 0 && !st[cur].have\_next(t[i])) {

                cur = st[cur].link;

                l = st[cur].len;

            }

            if (st[cur].have\_next(t[i])) {

                cur = st[cur].next[t[i]];

                l++;

            }

            if (l > mx) {

                mx = l;

                idx = i;

            }

        }

        return t.substr(idx - mx + 1, mx);

    }

};

## Suffix array

class suffix\_array {

    int getOrder(int a) const {

        return (a < (int) order.size() ? order[a] : 0);

    }

    void radix\_sort(int k) {

        vector<int> frq(n), tmp(n);

        for (auto &it : suf)

            frq[getOrder(it + k)]++;

        for (int i = 1; i < n; i++)

            frq[i] += frq[i - 1];

        for (int i = n - 1; i >= 0; i--)

            tmp[--frq[getOrder(suf[i] + k)]] = suf[i];

        suf = tmp;

    }

public:

    int n;

    string s;

    vector<int> suf, lcp, order; // order store position of suffix i in suf array

    suffix\_array(const string &s) :

            n(s.size() + 1), s(s) {

        suf = order = vector<int>(n);

        vector<int> newOrder(n);

        for (int i = 0; i < n; i++)

            suf[i] = i;

        { //sort according to first character

            vector<int> tmp(n);

            for (int i = 0; i < n; i++)

                tmp[i] = s[i];

            sort(all(tmp));

            for (int i = 0; i < n; i++)

                order[i] = (lower\_bound(all(tmp), s[i]) - tmp.begin());

        }

        for (int len = 1; newOrder.back() != n - 1; len <<= 1) {

            auto cmp = [&](const int &a, const int &b) {

                if (order[a] != order[b])

                    return order[a] < order[b];

                return getOrder(a + len) < getOrder(b + len);

            };

            //sort(all(suf), cmp); //run in 576ms  (n<=4e5)

            radix\_sort(len); //sort second part

            radix\_sort(0); //sort first part

            newOrder[0] = 0;

            for (int i = 1; i < n; i++)

                newOrder[i] = newOrder[i - 1] + cmp(suf[i - 1], suf[i]);

            for (int i = 0; i < n; i++)

                order[suf[i]] = newOrder[i];

        }

        buildLCP();

    }

    /\*

     \* longest common prefix

     \* O(n)

     \* lcp[i] = lcp(suf[i],suf[i-1])

     \*/

    void buildLCP() {

        lcp = vector<int>(n);

        int k = 0;

        for (int i = 0; i < n - 1; i++) {

            int pos = order[i];

            int j = suf[pos - 1];

            while (s[i + k] == s[j + k])

                k++;

            lcp[pos] = k;

            if (k)

                k--;

        }

    }

    int LCP\_by\_order(int a, int b) {

        if (a > b)

            swap(a, b);

        int mn = n - suf[a] - 1;

        for (int k = a + 1; k <= b; k++)

            mn = min(mn, lcp[k]);

        return mn;

    }

    //LCP(i,j) : longest common prefix between suffix i and suffix j

    int LCP(int i, int j) {

        //return LCP\_by\_order(order[i],order[j]);

        if (order[j] < order[i])

            swap(i, j);

        int mn = n - i - 1;

        for (int k = order[i] + 1; k <= order[j]; k++)

            mn = min(mn, lcp[k]);

        return mn;

    }

    //compare s[a.first..a.second] with s[b.first..b.second]

    //-1:a<b ,0:a==b,1:a>b

    int compare\_substrings(pair<int, int> a, pair<int, int> b) {

        int lcp = min({ LCP(a.first, b.first), a.second - a.first + 1, b.second - b.first + 1 });

        a.first += lcp;

b.first += lcp;

        if (a.first <= a.second) {

            if (b.first <= b.second) {

                if (s[a.first] == s[b.first])

                    return 0;

                return (s[a.first] < s[b.first] ? -1 : 1);

            }

            return 1;

        }

        return (b.first <= b.second ? -1 : 0);

    }

    pair<int, int> find\_string(const string &x) {

        int st = 0, ed = n;

        for (int i = 0; i < sz(x) && st < ed; i++) {

            auto cmp = [&](int a, int b) {

                if (a == -1)

                    return x[i] < s[b + i];

                return s[a + i] < x[i];

            };

            st = lower\_bound(suf.begin() + st, suf.begin() + ed, -1, cmp)

                    - suf.begin();

            ed = upper\_bound(suf.begin() + st, suf.begin() + ed, -1, cmp)

                    - suf.begin();

        }

        return {st,ed-1};

    }

};

ll number\_of\_different\_substrings(string s) {

    int n = s.size();

    suffix\_array sa(s);

    ll cnt = 0;

    for (int i = 0; i <= n; i++)

        cnt += n - sa.suf[i] - sa.lcp[i];

    return cnt;

}

string longest\_common\_substring(const string &s1, const string &s2) {

    suffix\_array sa(s1 + "#" + s2);

    vector<int> suf = sa.suf, lcp = sa.lcp;

    auto type = [&](int idx) {

        return idx <= s1.size();

    };

    int mx = 0, idx = 0;

    int len = s1.size() + 1 + s2.size();

    for (int i = 1; i <= len; i++)

        if (type(suf[i - 1]) != type(suf[i]) && lcp[i] > mx) {

            mx = lcp[i];

            idx = min(suf[i - 1], suf[i]);

        }

    return s1.substr(idx, mx);

}

int longest\_common\_substring(const vector<string> &v) {

    int n = v.size();

    int len = n - 1;

    for (auto &it : v)

        len += it.size();

    string s(len, '.');

    vector<int> type(len + 1, n), frq(n + 1);

    for (int i = 0, j = 0; i < v.size(); i++) {

        if (i)

            s[j] = 'z' + i;

        for (char ch : v[i]) {

            s[j] = ch;

            type[j] = i;

            j++;

        }

    }

    suffix\_array sa(s);

    vector<int> suf = sa.suf, lcp = sa.lcp;

    monoqueue q;

    int st = 0, ed = 0, cnt = 0, mx = 0;

    while (st <= s.size()) {

        while (ed <= s.size() && cnt < v.size()) {

            q.push(lcp[ed], ed);

            if (++frq[type[suf[ed]]] == 1)

                cnt++;

            ed++;

        }

        q.pop(st);

        if (cnt == v.size())

            mx = max(mx, q.getMin()); //st+1,ed

        if (--frq[type[suf[st]]] == 0)

            cnt--;

        st++;

    }

    return mx;

}

string kth\_substring(string s, int k) { //1-based,repated

    int n = s.size();

    suffix\_array sa(s);

    vector<int> suf = sa.suf, lcp = sa.lcp;

    for (int i = 1; i <= n; i++) {

        int len = n - suf[i];

        int cnt = 0;

        for (int l = 1; l <= len; l++) {

            cnt++;

            int st = i + 1, ed = n, ans = i;

            while (st <= ed) {

                int md = st + ed >> 1;

                if (sa.LCP\_by\_order(i, md) >= l)

                    st = md + 1, ans = md;

                else

                    ed = md - 1;

            }

            cnt += ans - i;

            if (cnt >= k)

                return s.substr(suf[i], l);

        }

        k -= len;

    }

    assert(0);

}

### Suffix array Faster

class suffix\_array {

    const static int alpha = 128;

    int getOrder(int a) const {

        return (a < (int) order.size() ? order[a] : 0);

    }

public:

    int n;

    string s;

    vector<int> suf, order, lcp; // order store position of suffix i in suf array

    suffix\_array(const string &s) : n(s.size() + 1), s(s) {

        suf = order = lcp = vector<int>(n);

        vector<int> bucket\_idx(n), newOrder(n), newsuff(n);

        vector<int> prev(n), head(alpha, -1);

        for (int i = 0; i < n; i++) {

            prev[i] = head[s[i]];

            head[s[i]] = i;

        }

        int buc = -1, idx = 0;

        for (int i = 0; i < alpha; i++) {

            if (head[i] == -1)

                continue;

            bucket\_idx[++buc] = idx;

            for (int j = head[i]; ~j; j = prev[j])

                suf[idx++] = j, order[j] = buc;

        }

        int len = 1;

        do {

            auto cmp = [&](int a, int b) {

                if (order[a] != order[b])

                    return order[a] < order[b];

                return getOrder(a + len) < getOrder(b + len);

            };

            for (int i = 0; i < n; i++) {

                int j = suf[i] - len;

                if (j < 0)

                    continue;

                newsuff[bucket\_idx[order[j]]++] = j;

            }

            for (int i = 1; i < n; i++) {

                suf[i] = newsuff[i];

                bool cmpres = cmp(suf[i - 1], suf[i]);

                newOrder[suf[i]] = newOrder[suf[i - 1]] + cmpres;

                if (cmpres)

                    bucket\_idx[newOrder[suf[i]]] = i;

            }

            order = newOrder;

            len <<= 1;

        } while (order[suf[n - 1]] != n - 1);

    }

};

## Z algorithm

/\*

 \*   z[i] equal the length of the longest substring starting from s[i]

 \*    which is also a prefix of s

 \*/

vector<int> z\_algo(string s) {

    int n = s.size();

    vector<int> z(n);

    z[0] = n;

    for (int i = 1, L = 1, R = 1; i < n; i++) {

        int k = i - L;

        if (z[k] + i >= R) {

            L = i;

            R = max(R, i);

            while (R < n && s[R - L] == s[R])

                R++;

            z[i] = R - L;

        } else

            z[i] = z[k];

    }

    return z;

}

# Math

## Combinatorics

/\*

\* nCr = n!/((n-r)! \* r!)

\* nCr(n,r) = nCr(n,n-r)

\* nPr = n!/(n-r)!

\* nPr(circle) = nPr/r

\* nCr(n,r) = pascal[n][r]

\* catalan[n] = nCr(2n,n)/(n+1)

\*/

ull nCr(int n, int r) {

if (r > n)

return 0;

r = max(r, n - r);

ull ans = 1, div = 1, i = r + 1;

while (i <= n) {

ans \*= i++;

ans /= div++;

}

return ans;

}

ull nPr(int n, int r) {

if (r > n)

return 0;

ull p = 1, i = n - r + 1;

while (i <= n)

p \*= i++;

return p;

}

vector<vector<ull>> pascalTriangle(int n) {

vector<vector<ull>> pascal(n + 1, vector<ull>(n + 1));

for (int i = 0; i <= n; i++) {

pascal[i][i] = pascal[i][0] = 1;

for (int j = 1; j < n; j++)

pascal[i][j] = pascal[i - 1][j] + pascal[i - 1][j - 1];

}

return pascal;

}

// return catalan number n-th using dp O(n^2)//max = 35 then overflow

vector<ull> catalanNumber(int n) {

vector<ull> catalan(n + 1);

catalan[0] = catalan[1] = 1;

for (int i = 2; i <= n; i++) {

ull& rt = catalan[i];

for (int j = 0; j < n; j++)

rt += catalan[j] \* catalan[n - j - 1];

}

return catalan;

}

// count number of paths in matrix n\*m

// go to right or down only

ull countNumberOfPaths(int n, int m) {

return nCr(n + m - 2, n - 1);

}

## NCR pre calculation

const int N = 1e5 + 100;

const int mod = 1e9 + 7;

ll fact[N];

ll inv[N]; //mod inverse for i

ll invfact[N]; //mod inverse for i!

void factInverse() {

fact[0] = inv[1] = fact[1] = invfact[0] = invfact[1] = 1;

for (long long i = 2; i < N; i++) {

fact[i] = (fact[i - 1] \* i) % mod;

inv[i] = mod - (inv[mod % i] \* (mod / i) % mod);

invfact[i] = (inv[i] \* invfact[i - 1]) % mod;

}

}

ll nCr(int n, int r) {

if (r > n)

return 0;

return (((fact[n] \* invfact[r]) % mod) \* invfact[n - r]) % mod;

}

## Matrices

typedef vector<int> row;

typedef vector<row> matrix;

matrix initial(int n, int m, int val = 0) {

return matrix(n, row(m, val));

}

matrix identity(int n) {

matrix rt = initial(n, n);

for (int i = 0; i < n; i++)rt[i][i] = 1;

return rt;

}

matrix addIdentity(const matrix& a) {

matrix rt = a;

for (int i = 0; i < sz(a); i++)rt[i][i] += 1;

return rt;

}

matrix add(const matrix& a, const matrix& b) {

matrix rt = initial(sz(a), sz(a[0]));

for (int i = 0; i < sz(a); i++)for (int j = 0; j < sz(a[0]); j++)

rt[i][j] = a[i][j] + b[i][j];

return rt;

}

matrix multiply(const matrix& a, const matrix& b) {

matrix rt = initial(sz(a), sz(b[0]));

for (int i = 0; i < sz(a); i++) for (int k = 0; k < sz(a[0]); k++) {

if (a[i][k] == 0)continue;

for (int j = 0; j < sz(b[0]); j++)

rt[i][j] += a[i][k] \* b[k][j];

}

return rt;

}

matrix power(const matrix& a, ll k) {

if (k == 0)return identity(sz(a));

if (k & 1)return multiply(a, power(a, k - 1));

return power(multiply(a, a), k >> 1);

}

matrix power\_itr(matrix a, ll k) {

matrix rt = identity(sz(a));

while (k) {

if (k & 1)rt = multiply(rt, a);

a = multiply(a, a); k >>= 1;

}

return rt;

}

matrix sumPower(const matrix& a, ll k) {

if (k == 0)return initial(sz(a), sz(a));

if (k & 1)return multiply(a, addIdentity(sumPower(a, k - 1)));

return multiply(sumPower(a, k >> 1), addIdentity(power(a, k >> 1)));

}

matrix sumPowerV2(const matrix& a, ll k) {

int n = sz(a);

matrix rt = initial(2 \* n, 2 \* n);

for (int i = 0; i < 2 \* n; i++)

for (int j = 0; j < n; j++)

rt[i][j] = a[i % n][j];

for (int i = n; i < 2 \* n; i++)rt[i][i] = 1;

return power(rt, k);

}

### Matrix class

struct matrix {

using T = int;

using row = vector<T>;

vector<vector<T>> v;

matrix() {}

matrix(int n, int m, T val = 0) : v(n, row(m, val)) {

}

int size() const {

return v.size();

}

int cols() const {

return v[0].size();

}

matrix operator\*(T a) const {

matrix rt = \*this;

REP(i, rt.size())

REP(j, rt.cols())

rt.v[i][j] \*= a;

return rt;

}

friend matrix operator\*(T a, const matrix& b) {

return (b \* a);

}

friend matrix operator+(const matrix& a, const matrix& b) {

assert(a.size() == b.size() && a.cols() == b.cols());

matrix rt(a.size(), a.cols());

REP(i, rt.size())

REP(j, rt.cols())

rt.v[i][j] = a.v[i][j] + b.v[i][j];

return rt;

}

friend matrix operator\*(const matrix& a, const matrix& b) {

assert(a.cols() == b.size());

matrix rt(a.size(), b.cols());

REP(i, rt.size())

REP(k, a.cols())

{

if (a.v[i][k] == 0)

continue;

REP(j, rt.cols())

rt.v[i][j] += a.v[i][k] \* b.v[k][j];

}

return rt;

}

};

matrix identity(int n) {

matrix r(n, n);

for (int i = 0; i < n; i++)

r.v[i][i] = 1;

return r;

}

matrix power(matrix a, long long y) {

assert(y >= 0 && a.size() == a.cols());

matrix rt = identity(a.size());

while (y > 0) {

if (y & 1)

rt = rt \* a;

a = a \* a;

y >>= 1;

}

return rt;

}

matrix addIdentity(const matrix& a) {

matrix rt = a;

REP(i, a.size())

rt.v[i][i]++;

return rt;

}

matrix sumPower(const matrix& a, ll k) {

if (k == 0)

return matrix(sz(a), sz(a));

if (k & 1)

return a \* addIdentity(sumPower(a, k - 1));

return (sumPower(a, k >> 1) \* addIdentity(power(a, k >> 1)));

}

matrix sumPowerV2(const matrix& a, ll k) {

int n = sz(a);

matrix rt(2 \* n, 2 \* n);

REP(i, n)

REP(j, n)

{

rt.v[i][j] = a.v[i][j];

rt.v[i + n][j] = a.v[i][j];

}

for (int i = n; i < 2 \* n; i++)

rt.v[i][i] = 1;

return power(rt, k);

}

## Mod inverse

ll power(ll x, ll y, int mod) {

    if (y == 0)

        return 1;

    if (y == 1)

        return x % mod;

    ll r = power(x, y >> 1, mod);

    return (((r \* r) % mod) \* power(x, y & 1, mod)) % mod;

}

ll modInverse(ll b, ll mod) { // if mod is Prime

    return power(b, mod - 2, mod);

}

ll modInverse(ll b, ll mod) { // if mod is not Prime,g(a,b) must be equal 1

    return power(b, phi\_function(mod) - 1, mod);

}

//ax + by = gcd(a, b)

int gcdExtended(int a, int b, int &x, int &y) {

    if (a == 0) {

        x = 0;

        y = 1;

        return b;

    }

    int x1, y1;

    int g = gcdExtended(b % a, a, x1, y1);

    x = y1 - (b / a) \* x1;

    y = x1;

    return g;

}

int modInverse(int a, int mod) {

    int x, y;

    int g = gcdExtended(a, mod, x, y);

    assert(g == 1);

    x = (x % mod + mod) % mod;

    return x;

}

template<typename T>

T inverse(T a, T m) { //tourist code

    T u = 0, v = 1;

    while (a != 0) {

        T t = m / a;

        m -= t \* a;

        swap(a, m);

        u -= t \* v;

        swap(u, v);

    }

    assert(m == 1);

    return u;

}

## (a^n)%p=result , return n

// (a^n)%p=result,return minimum n

int getPower(int a, int result, int mod) {

int sq = sqrt(mod);

map<int, int> mp;

ll r = 1;

for (int i = 0; i < sq; i++) {

if (mp.find(r) == mp.end())

mp[r] = i;

r = (r \* a) % mod;

}

ll tmp = modInverse(r, mod);

ll cur = result;

for (int i = 0; i <= mod; i += sq) {

if (mp.find(cur) != mp.end())

return i + mp[cur];

cur = (cur \* tmp) % mod;//val/(a^sq)

}

return INF;

}

// Returns minimum x for which a ^ x % m = b % m.

// a,m not not coprime

**int** **getPower**(**int** a, **int** b, **int** m) {

a %= m, b %= m;

**int** k = 1, add = 0, g;

**while** ((g = \_\_gcd(a, m)) > 1) {

**if** (b == k)

**return** add;

**if** (b % g)

**return** -1;

b /= g, m /= g, ++add;

k = (k \* 1ll \* a / g) % m;

}

**int** n = sqrt(m) + 1;

**int** an = 1;

**for** (**int** i = 0; i < n; ++i)

an = (an \* 1ll \* a) % m;

unordered\_map<**int**, **int**> vals;

**for** (**int** q = 0, cur = b; q <= n; ++q) {

vals[cur] = q;

cur = (cur \* 1ll \* a) % m;

}

**for** (**int** p = 1, cur = k; p <= n; ++p) {

cur = (cur \* 1ll \* an) % m;

**if** (vals.count(cur)) {

**int** ans = n \* p - vals[cur] + add;

**return** ans;

}

}

**return** -1;

}

## Primes

typedef vector<pair<ll, int>> primeFactors;

const int N = 1e8;

bool isPrime[N + 1];

vector<int> prime;

void sieve() {

memset(isPrime, true, sizeof(isPrime));

isPrime[0] = isPrime[1] = false;

for (int i = 4; i <= N; i += 2)

isPrime[i] = false;

for (int i = 3; i \* i <= N; i += 2)

if (isPrime[i])

for (int j = i \* i; j <= N; j += i + i)

isPrime[j] = false;

for (int i = 1; i <= N; i++)

if (isPrime[i])

prime.push\_back(i);

}

// generate prime divisors in n

// n = p1^x1 \* p2^x2 .... pn^xn

// O(sqrt(n)) // max = 1e16

primeFactors prime\_factors(ll n) {

primeFactors p;

int idx = 0;

while (!(n <= N && isPrime[n]) && idx < prime.size()

&& 1LL \* prime[idx] \* prime[idx] <= n) {

int cnt = 0;

while (n % prime[idx] == 0)

n /= prime[idx], cnt++;

if (cnt)

p.push\_back({ prime[idx], cnt });

idx++;

}

if (n > 1)

p.push\_back({ n, 1 });

return p;

}

// return number of Divisors(n) using prime factorization

ll numOfDivisors(primeFactors mp) {

ll cnt = 1;

for (auto it : mp)

cnt \*= (it.second + 1);

return cnt;

}

// return sum of Divisors(n) using prime factorization

ll sumOfDivisors(primeFactors mp) {

ll sum = 1;

for (auto it : mp)

sum \*= sumPower(it.first, it.second);

return sum;

}

ll phi\_function(ll n) {

ll result = n;

primeFactors pf = prime\_factors(n);

for (auto& it : pf) {

ll p = it.first;

result -= (result / p);

}

return result;

}

## Summations

#define numOfDigit(x) 1+(int)(floor(log10(x)))

#define numOfBits(x) 1+(int)(floor(log2(x)))

//return sum of sequence a, a+x , a+2x .... b

ll sumSequence(ll a, ll b, ll x) {

a = ((a + x - 1) / x) \* x;

b = (b / x) \* x;

return (b + a) \* (b - a + x) / (2 \* x);

}

ll sumPower(ll x, ll y) { //x^0 + x^1 + x^2 ... x^y

return (power(x, y + 1) - 1) / (x - 1);

}

// return sum of divisors for all number from 1 to n

//O(n)

ll sumRangeDivisors(int n) {

ll ans = 0;

for (int x = 1; x <= n; x++)

ans += (n / x) \* x;

return ans;

}

// return sum of divisors for all number from 1 to n

// calc 1e9 in 42ms,can calc more but need big integer

ll sumRangeDivisors(ll x) {

ll ans = 0, left = 1, right;

for (; left <= x; left = right + 1) {

right = x / (x / left);

ans += (x / left) \* (left + right) \* (right - left + 1) / 2;

}

return ans;

}

 \* sum of q^0 + q^1 + q^2 ... q^INF = 1/q if (0<q<1)

## Calculator

bool delim(char c) {

    return c == ' ';

}

bool is\_op(char c) {

    return c == '+' || c == '-' || c == '\*' || c == '/';

}

bool is\_unary(char c) {

    return c == '+' || c=='-';

}

int priority (char op) {

    if (op < 0) // unary operator

        return 3;

    if (op == '+' || op == '-')

        return 1;

    if (op == '\*' || op == '/')

        return 2;

    return -1;

}

void process\_op(stack<int>& st, char op) {

    if (op < 0) {

        int l = st.top(); st.pop();

        switch (-op) {

            case '+': st.push(l); break;

            case '-': st.push(-l); break;

        }

    } else {

        int r = st.top(); st.pop();

        int l = st.top(); st.pop();

        switch (op) {

            case '+': st.push(l + r); break;

            case '-': st.push(l - r); break;

            case '\*': st.push(l \* r); break;

            case '/': st.push(l / r); break;

        }

    }

}

int evaluate(string& s) {

    stack<int> st;

    stack<char> op;

    bool may\_be\_unary = true;

    for (int i = 0; i < (int)s.size(); i++) {

        if (delim(s[i]))

            continue;

        if (s[i] == '(') {

            op.push('(');

            may\_be\_unary = true;

        } else if (s[i] == ')') {

            while (op.top() != '(') {

                process\_op(st, op.top());

                op.pop();

            }

            op.pop();

            may\_be\_unary = false;

        } else if (is\_op(s[i])) {

            char cur\_op = s[i];

            if (may\_be\_unary && is\_unary(cur\_op))

                cur\_op = -cur\_op;

            while (!op.empty() && (

                    (cur\_op >= 0 && priority(op.top()) >= priority(cur\_op)) ||

                    (cur\_op < 0 && priority(op.top()) > priority(cur\_op))

                )) {

                process\_op(st, op.top());

                op.pop();

            }

            op.push(cur\_op);

            may\_be\_unary = true;

        } else {

            int number = 0;

            while (i < (int)s.size() && isalnum(s[i]))

                number = number \* 10 + s[i++] - '0';

            --i;

            st.push(number);

            may\_be\_unary = false;

        }

    }

    while (!op.empty()) {

        process\_op(st, op.top());

        op.pop();

    }

    return st.top();

}

# Misc

## Bitmask

bool getBit(ll num, int ind) {

return ((num >> ind) & 1);

}

ll setBit(ll num, int ind, bool val) {

return val ? (num | (1LL << ind)) : (num & ~(1LL << ind));

}

ll flipBit(ll num, int ind) {

return (num ^ (1LL << ind));

}

ll leastBit(ll num) {

return (num & -num);

}

template<class Int>

Int turnOnLastZero(Int num) {

return num | num + 1;

}

template<class Int>

Int turnOnLastConsecutiveZeroes(Int num) {

return num | num - 1;

}

template<class Int>

Int turnOffLastBit(Int num) {

return num & num - 1;

}

template<class Int>

Int turnOffLastConsecutiveBits(Int num) {

return num & num + 1;

}

//num%mod, mod is a power of 2

ll Mod(ll num, ll mod) {

return (num & mod - 1);

}

bool isPowerOfTwo(ll num) {

return (num & num - 1) == 0;

}

void genAllSubmask(int mask) {

for (int subMask = mask;; subMask = (subMask - 1) & mask) {

//code

if (subMask == 0)

break;

}

}

/\*

\* \_\_builtin functions:

\* \_\_builtin\_popcount -> used to count the number of one’s

\* \_\_builtin\_clz -> used to count the leading zeros of the integer

\* \_\_builtin\_ctz -> used to count the trailing zeros of the integer

\*

int LOG2(int x) { //floor(log2(x))

return 31 - \_\_builtin\_clz(x);

}

int LOG2(long long x) { //floor(log2(x))

return 63 - \_\_builtin\_clzll(x);

}

## coordinateCompress

void coordinateCompress(vector<int>& axes, vector<int>& iToV,

map<int, int> vToI, int start = 2, int step = 2) {

for (auto& it : axes)

vToI[it] = 0;

iToV.resize(start + step \* vToI.size());

int idx = 0;

for (auto& it : vToI) {

it.second = start + step \* idx;

iToV[it.second] = it.first;

idx++;

}

}

## Random numbers

//write this line once in top

mt19937\_64 rng(chrono::steady\_clock::now().time\_since\_epoch().count()\* ((uint64\_t) new char | 1));

// use this instead of rand()

long long rnd = uniform\_int\_distribution<long long>(low, high)(rng);

## Custom hash

struct custom\_hash {

static uint64\_t splitmix64(uint64\_t x) {

x += 0x9e3779b97f4a7c15;

x = (x ^ (x >> 30)) \* 0xbf58476d1ce4e5b9;

x = (x ^ (x >> 27)) \* 0x94d049bb133111eb;

return x ^ (x >> 31);

}

// for pair

size\_t operator()(pair<uint64\_t, uint64\_t> x) const {

static const uint64\_t FIXED\_RANDOM = chrono::steady\_clock::now().time\_since\_epoch().count();

return splitmix64(x.first + FIXED\_RANDOM) ^ (splitmix64(x.second + FIXED\_RANDOM) >> 1);

}

// for single element

size\_t operator()(uint64\_t x) const {

static const uint64\_t FIXED\_RANDOM = chrono::steady\_clock::now().time\_since\_epoch().count();

return splitmix64(x + FIXED\_RANDOM);

}

};

## Max histogram area

int maxHistogramArea(vector<int> v) {

stack<int> st;

int maxArea = 0, area = 0;

int i = 0;

while (i < sz(v)) {

if (st.empty() || v[st.top()] <= v[i])

st.push(i++);

else {

int top = st.top(); st.pop();

if (st.empty())

area = v[top] \* i;

else

area = v[top] \* (i - st.top() - 1);

maxArea = max(maxArea, area);

}

}

while (!st.empty()) {

int top = st.top(); st.pop();

if (st.empty())

area = v[top] \* i;

else

area = v[top] \* (i - st.top() - 1);

maxArea = max(maxArea, area);

}

return maxArea;

}

## Sorting

long long cnt = 0;

vector<int> v, temp;

// e the first index not have in range array

// like end()

template<class T = less<int>>

void merge\_sort(int s, int e, T cmp = less<int>()) {

if (s + 1 >= e)

return;

int m = s + (e - s >> 1);

merge\_sort(s, m, cmp);

merge\_sort(m, e, cmp);

for (int i = s; i < e; i++)

temp[i] = v[i];

int i = s, j = m, k = s;

while (i < m && j < e)

if (cmp(temp[i], temp[j]))

v[k++] = temp[i++];

else

v[k++] = temp[j++], cnt += j - k;

while (i < m)

v[k++] = temp[i++];

while (j < e)

v[k++] = temp[j++];

}

// O(n\*log(n)/log(base))

// O(n + base) memory

void radix\_sort(vector<int>& v, int base) {

vector<int> tmp(v.size());

for (int it = 0, p = 1; it < 10; it++, p \*= base) {

vector<int> frq(base);

for (auto& it : v)

frq[(it / p) % base]++;

for (int i = 1; i < base; i++)

frq[i] += frq[i - 1];

for (int i = v.size() - 1; i >= 0; i--)

tmp[--frq[(v[i] / p) % base]] = v[i];

v = tmp;

}

}

void quick\_sort(int s, int e) {

if (s >= e)

return;

int j = rand() % (e - s + 1) + s;

swap(v[s], v[j]);

j = s;

int pivot = v[s];

for (int i = s + 1; i <= e; i++)

if (v[i] <= pivot)

swap(v[i], v[++j]);

swap(v[s], v[j]);

quick\_sort(s, j - 1);

quick\_sort(j + 1, e);

}

## LIS binary Search

/\* without build

\* make upper\_bound if can take equal elements \*/

int LIS(const vector<int>& v) {

vector<int> lis(v.size());//put value less than zero if needed

int l = 0;

for (int i = 0; i < sz(v); i++) {

int idx = lower\_bound(lis.begin(), lis.begin() + l, v[i]) - lis.begin();

if (idx == l)

l++;

lis[idx] = v[i];

}

return l;

}

void LIS\_binarySearch(vector<int> v) {

int n = v.size();

vector<int> last(n), prev(n, -1);

int length = 0;

auto BS = [&](int val) {

int st = 1, ed = length, md, rt = length;

while (st <= ed) {

md = st + ed >> 1;

if (v[last[md]] >= val)

ed = md - 1, rt = md;

else st = md + 1;

}

return rt;

};

for (int i = 1; i < n; i++) {

if (v[i] < v[last[0]])

last[0] = i;

else if (v[i] > v[last[length]]) {

prev[i] = last[length];

last[++length] = i;

}

else {

int index = BS(v[i]);

prev[i] = last[index - 1];

last[index] = i;

}

}

cout << length + 1 << "\n";

vector<int> out;

for (int i = last[length]; i >= 0; i = prev[i])

out.push\_back(v[i]);

reverse(out.begin(), out.end());

for (auto it : out)

cout << it << endl;

}

## Mo algorithm

int sqrtN; //use a constent value

struct query {

int l, r, qIdx, block;

query(int l, int r, int qIdx) :

l(l), r(r), qIdx(qIdx), block(l / sqrtN) {

}

bool operator <(const query& o) const {

if (block != o.block)

return block < o.block;

return (block % 2 == 0 ? r < o.r : r > o.r);

}

};

int curL, curR, ans;

vector<query> q;

void add(int index);

void remove(int index);

void solve(int l, int r) {

while (curL > l)

add(--curL);

while (curR < r)

add(++curR);

while (curL < l)

remove(curL++);

while (curR > r)

remove(curR--);

}

vector<int> MO(int n) {

vector<int> rt(q.size());

ans = curL = curR = 0;

add(0);

sort(q.begin(), q.end());

for (auto it : q) {

solve(it.l, it.r);

rt[it.qIdx] = ans;

}

return rt;

}

## floyd cycle detection algorithm

template<class IntFunction>

pair<int, int> find\_cycle\_floyd(IntFunction f, int x0) {

int tortoise = f(x0), hare = f(f(x0));

while (tortoise != hare) {

tortoise = f(tortoise);

hare = f(f(hare));

}

int start = 0;

tortoise = x0;

while (tortoise != hare) {

tortoise = f(tortoise);

hare = f(hare);

start++;

}

int length = 1;

hare = f(tortoise);

while (tortoise != hare) {

hare = f(hare);

length++;

}

return make\_pair(start, length);

}

# Convex Hull Trick

struct Line {

    ll m, c;

    mutable ll p; //p is intersection between cur and next

    bool operator<(const Line &o) const {

        //change to (m>o.m,c < o.c) to get min

        if (m != o.m)

            return m < o.m;

        return c > o.c;

    }

    bool operator<(ll x) const {

        return p < x;

    }

};

struct LineContainer: multiset<Line, less<>> {

    // (for doubles, use inf = 1/.0, div(a,b) = a/b)

    static const ll inf = LLONG\_MAX;

    ll div(ll a, ll b) { // floored division

        return a / b - ((a ^ b) < 0 && a % b);

    }

    bool isect(iterator x, iterator y) {

        if (y == end())

            return x->p = inf, 0;

        if (x->m == y->m)

            x->p = inf;

        else

            x->p = div(y->c - x->c, x->m - y->m);

        return x->p >= y->p;

    }

    void add(ll m, ll c) {

        auto z = insert( { m, c, 0 }), y = z++, x = y;

        while (isect(y, z))

            z = erase(z);

        if (x != begin() && isect(--x, y))

            isect(x, y = erase(y));

        while ((y = x) != begin() && (--x)->p >= y->p)

            isect(x, erase(y));

    }

    ll query(ll x) {

        assert(!empty());

        auto l = \*lower\_bound(x);

        return l.m \* x + l.c;

    }

};

# Geometry

typedef complex<long double> point;

#define sz(a) ((int)(a).size())

#define all(n) (n).begin(),(n).end()

#define EPS 1e-9

#define OO 1e9

#define PI acos(-1.0)

#define X real()

#define Y imag()

#define vec(a,b) ((b)-(a))

#define polar(r,t) ((r)\*exp(point(0,(t))))

#define angle(v) (atan2((v).Y,(v).X))

#define length(v) ((long double)hypot((v).Y,(v).X))

#define lengthSqr(v) (dot(v,v))

#define dot(a,b) ((conj(a)\*(b)).real())

#define cross(a,b) ((conj(a)\*(b)).imag())

#define rotate(v,t) (polar(v,t))

#define rotateabout(v,t,a) (rotate(vec(a,v),t)+(a))

#define reflect(p,m) ((conj((p)/(m)))\*(m))

#define normalize(p) ((p)/length(p))

#define same(a,b) (lengthSqr(vec(a,b))<EPS)

#define mid(a,b) (((a)+(b))/point(2,0))

#define perp(a) (point(-(a).Y,(a).X))

#define colliner pointOnLine

enum STATE {IN, OUT, BOUNDRY};

int dcmp(double x, double y) { return fabs(x - y) <= EPS ? 0 : x < y ? -1 : 1; }

double fixAngle(double A) { return A > 1 ? 1 : (A < -1 ? -1 : A);}

double fixMod(double a, double b) {return fmod(fmod(a, b) + b, b);}

## **pointOnLine**

bool pointOnLine(const point& a, const point& b, const point& p) {

return fabs(cross(vec(a, b), vec(a, p))) < EPS;

}

## pointOnRay

inline bool pointOnRay(point a, point b, point p) {

return dot(vec(a, b), vec(a, p)) > -EPS && pointOnLine(a, b, p);

}

## pointOnSegment

inline bool pointOnSegment(point a, point b, point p) {

return dot(vec(a, b), vec(a, p)) > -EPS && pointOnLine(a, b, p) && dot(vec(b, a), vec(b, p)) > -EPS;

}

## return y of point on line given the line and x of this point

long double getYfromXforline(point a, point b, long double x) {

if (a.X == b.X)return b.Y;

long double m = (a.Y - b.Y) / (a.X - b.X);

long double c = a.Y - m \* a.X;

return m \* x + c;

}

return x of point on line given the line and y of this point

long double getXfromYforline(point a, point b, long double y) {

if (a.X == b.X)return b.X;

long double m = (a.Y - b.Y) / (a.X - b.X);

long double c = a.Y - m \* a.X;

return (y - c) / m;

}

namespace std {

bool operator <(const point& a, const point& b) {

return a.X != b.X ? a.X < b.X : a.Y < b.Y;

}

bool operator >(const point& a, const point& b) {

return a.X != b.X ? a.X > b.X : a.Y > b.Y;

}

// sortsegments butome up , note the point of 1 segment must be sorted

// the functions that coled must be up of this poisition in code

bool operator <(const vector<point>& a, const vector<point>& b) {

point p(a[0].X, getYfromXforline(b[0], b[1], a[0].X));

if (pointOnSegment(b[0], b[1], p))return a[0].Y < p.Y;

p = point(a[1].X, getYfromXforline(b[0], b[1], a[1].X));

if (pointOnSegment(b[0], b[1], p))return a[1] < p;

p = point(b[0].X, getYfromXforline(a[0], a[1], b[0].X));

if (pointOnSegment(a[0], a[1], p))return p < b[0];

p = point(b[1].X, getYfromXforline(a[0], a[1], b[1].X));

if (pointOnSegment(a[0], a[1], p))return p < b[1];

return max(a[0].Y, a[1].Y) < max(b[0].Y, b[1].Y);

}

}

## return the y of a point that falling up segments untile it fall to ground (as water fall)

double waterFallOnsegments(vector< vector<point> > v, point p) {

for (int i = (int)v.size() - 1; i >= 0; i--) {

double x = p.X, y = getYfromXforline(v[i][0], v[i][1], p.X);

if (y <= p.Y&&pointOnSegment(v[i][0], v[i][1], point(x, y))) {

if (v[i][0].Y < v[i][1].Y)p = v[i][0];

else p = v[i][1];

}

}

return p.X;

}

point readpoint() { long double x, y; cin >> x >> y; return point(x, y); }

void printpoint(point P) { cout << P.X << " " << P.Y; }

// somtimes point is -0.0 it is ronge mmust be 0,0

void fixpoint(point &p) {

if (p.X<EPS&&p.X>-EPS)p = point(0, p.Y);

if (p.Y<EPS&&p.Y>-EPS)p = point(p.X, 0);

}

## prependecularVecor

bool prependecularVec(const point &a, const point &b) {

return dot(a, b) == 0;

}

## paralelVector

bool paralelVec(const point &a, const point &b) {

return cross(a, b) == 0;

}

## check if a point inside the rectangle

bool pointInsidReqt(point LD, point RU, point P) {

//note that ">= and <=" not "> and <" it based on your problem...

return P.X >= LD.X && P.X <= RU.X && P.Y >= LD.Y && P.Y <= RU.Y;

}

## check if a point inside the circle

bool pointInsidCircle(point center, long double rad, point P) {

long double d = length(vec(center, P));

return d<rad;//note that " < " not " <= " it based on your problem.......

}

## check if a point inside the triangle

bool pointInsidTrian(point P1, point P2, point P3, point P) {

long double A = fabs(cross(vec(P1, P2), vec(P1, P3)) / 2);

long double A1 = fabs(cross(vec(P, P2), vec(P, P3)) / 2);

long double A2 = fabs(cross(vec(P, P1), vec(P, P3)) / 2);

long double A3 = fabs(cross(vec(P, P1), vec(P, P2)) / 2);

//total area==areas of 3 triangles and the point is not in the porder =>>(A1>0 ,..)

return fabs(A - A1 - A2 - A3) < EPS&&A1&&A2&&A3;

}

## line using it’s a, b, c

struct line {

long double a, b, c;

line(point p1, point p2) {

if (abs(p1.X - p2.X) < EPS) { a = 1.0; b = 0.0; c = -p1.X; }

else {

a = -(long double)(p1.Y - p2.Y) / (p1.X - p2.X);

b = 1.0;

c = -(long double)(a \* p1.X) - p1.Y;

}

}

};

## Point To Segment

point pointToSegment(point p0, point p1, point p2) {

ld d1, d2;

point v1 = p1 - p0, v2 = p2 - p0;

if ((d1 = dp(v1, v2)) <= 0) return p0;

if ((d2 = dp(v1, v1)) <= d1) return p1;

ld t = d1 / d2;

return (p0 + v1 \* t);

}

## check if to lines are parallel

bool areParallel(line l1, line l2) {

return abs(l1.a - l2.a) < EPS && abs(l1.b - l2.b) < EPS;

}

## check if to lines are the same

bool areSame(line l1, line l2) {

return areParallel(l1, l2) && abs(l1.c - l2.c) < EPS;

}

## check if to lines are the same using points

bool samelLine(const point &a1, const point &b1,const point &a2, const point &b2)

{

return paralelVec(vec(a1,b1),vec(a2,b2))&&pointOnLine(a1,b1,a2);

}

## check if 2 lines are intersecting

int linIntersect(point a, point b, point p, point q, point &ret) {

line l1(a, b), l2(p, q);

if (areParallel(l1, l2)) return areSame(l1, l2) ? 2 : 0; // no intersection // solve system of 2 linear algebraic equations with 2 unknowns

double x, y;

x = (l2.b \* l1.c - l1.b \* l2.c) / (l2.a \* l1.b - l1.a \* l2.b);

// special case: test for vertical line to avoid division by zero

if (abs(l1.b) > EPS) y = -(l1.a \* x + l1.c);

else y = -(l2.a \* x + l2.c);

ret = point(x, y);

return 1;}

## get angle (AOB): in radian

double angl(point a, point o, point b) {

point oa = vec(o, a), ob = vec(o, b);

return acos(dot(oa, ob) / sqrt(norm\_sq(oa) \* norm\_sq(ob)));

}

// wr answer in team formation :D

double getAngle\_A\_abc(double a, double b, double c) {

return acos(fixAngle((b \* b + c \* c - a \* a) / (2 \* b \* c)));

}

// sin(A)/a = sin(B)/b = sin(C)/c

// a^2 = b^2 + c^2 - 2b\*c\*cos(A)

## Triangle side given other side and angle

double getSide\_a\_bAB(double b, double A, double B) {

return (sin(A) \* b) / sin(B);

}

## Triangle angel given other side and angle

double getAngle\_A\_abB(double a, double b, double B) {

return asin(fixAngle((a \* sin(B)) / b));

}

## Line Inside Rectangle

bool lineInsideRectangle(double x1, double x2, double y1, double y2, point st, point ed) {

if (x2 < x1) swap(x1, x2);

if (y2 < y1) swap(y1, y2);

double mnX = min(st.X, ed.X), mxX = max(st.X, ed.X),

mnY = min(st.Y, ed.Y), mxY = (st.Y, ed.Y);

return dcmp(x1, mnX) <= 0 && dcmp(x2, mxX) >= 0 && dcmp(y1, mnY) <= 0 && dcmp(y2, mxY) >= 0;

}

## check if 2 segments intersect

bool segmentIntersect(point a, point b, point p, point q, point &ret) {

int ans = linIntersect(a, b, p, q, ret);

if (ans == 0)return 0;

// if we check on ray we must use pointOnray() insted of pointOnSegment

if (ans == 1)return pointOnSegment(a, b, ret) && pointOnSegment(p, q, ret);

if (a > b)swap(a, b);

if (p > q)swap(p, q);

if (b < p || q < a)return 0;

ret = max(a, q); return 1;

}

## check if a line intersects with a rectangle using its (left dawn) and (right up) points

bool linReqtIntersect(point LD, point RU, point a, point b) {

point ret;

point LU = point(LD.X, RU.Y);

point RD = point(RU.X, LD.Y);

if (pointInsidReqt(LD, RU, a))return 1;

if (pointInsidReqt(LD, RU, b))return 1;

if (segmentIntersect(LU, RU, a, b, ret))return 1;

if (segmentIntersect(LD, RD, a, b, ret))return 1;

if (segmentIntersect(LD, LU, a, b, ret))return 1;

if (segmentIntersect(RD, RU, a, b, ret))return 1;

return 0;

}

double norm\_sq(point v) { return v.X \* v.X + v.Y \* v.Y; }

## convert the angle from degree to radian

double toRad(double d) { return (d \* PI) / 180.0; }

## convert the angle from radian to degree

double toDeg(double d) {

if (d < 0) d += 2 \* PI; return (d \* 180 / PI);

}

## find angle Anticlockwise from v1 to v2

double getAngle\_2vec(point v1, point v2) {

return toDeg(atan2(cross(v1, v2), dot(v1, v2)));

}

## find angle p2p0p1, anti-clock p0p1 to p0p2

double getAngle\_3points(point p0, point p1, point p2) {

return getAngle\_2vec(vec(p0, p1), vec(p0, p2));

}

## get vector as a point from it length and angle

point getvec(double r, double ang) {

//if the angle in degree

ang = toRad(ang);

double x = cos(ang)\*r;

double y = sin(ang)\*r;

return point(x, y);

}

point scale(point v, double r) {

return point(v.X\*r, v.Y\*r);

}

## get vector with length R according to a Ray ab

point getVectorWithLengthR(point a, point b, double r) {

return scale(normalize(vec(a, b)), r); }

## get triangle Area using 3 points

long double triangleArea3points(const point& a, const point& b, const point& c) {

return fabs(cross(a, b) + cross(b, c) + cross(c, a)) / 2;

}

## given the area of rectangle using 3 medians

double traingleArea\_medians(double m1, double m2, double m3) {

if (m1 <= 0.0 || m2 <= 0.0 || m3 <= 0.0)return -1; //impossipole

double s = 0.5\*(m1 + m2 + m3);

double midian\_area = (s\*(s - m1)\*(s - m2)\*(s - m3));

double area = 4.0 / 3.0\*sqrt(midian\_area);

if (midian\_area <= 0.0 || area <= 0.0)return -1;//impossipole

return area;

}

## check Overlapping Rectangles using (left down) and (right up) point for each

bool overlapReqt(point LD1, point RU1, point LD2, point RU2, point &LD3, point &RU3) {

long double x, y;

x = max(LD1.X, LD2.X);

y = max(LD1.Y, LD2.Y);

LD3 = point(x, y); // the left down poitn for the new rectangle

x = min(RU1.X, RU2.X);

y = min(RU1.Y, RU2.Y);

RU3 = point(x, y);// the left right up for the new rectangle

return LD3.X < RU3.X&&LD3.Y < RU3.Y;

}

## Given are the (x, y) coordinates of the endpoints of two adjacent sides of a parallelogram. Find the (x, y) coordinates of the fourth point.

point getForthPoint(point a1, point a2, point b1, point b2) {

if (same(a1, b1))return a2 + vec(b1, b2);

if (same(a1, b2))return a2 + vec(b2, b1);

if (same(a2, b1))return a1 + vec(b1, b2);

return a1 + vec(b2, b1);

}

get all possible points that complete the parallelogram with another 3 points(triangle)

vector<point> getParalel\_Tria(point p1, point p2, point p3) {

vector<point> v(3);

v[0] = p3 + vec(p2, p1);

v[1] = p1 + vec(p3, p2);

v[2] = p3 + vec(p1, p2);

return v;//each point from them can added to the old 3 points to get the paralelogram

}

## check if a polygon with angles = A is regular polygon

bool isRegulPoleg\_Angle(double A) {

for (int i = 3; i < 400; i++)

if (A == ((i - 2.0)\*180.0) / i)return 1;

return 0;

}

## Check if 4 point create a Rectangle

// the order needed colocwise

bool isRect(point a, point b, point c, point d){

return vec(a, b) == vec(d, c) && vec(a, d) == vec(b, c) && prependecularVec(vec(a, b), vec(a, d));

}

## Check if 4 point create a Square

// the order needed colocwise

bool isSquar(point a, point b, point c, point d){

return vec(a, b) == vec(d, c) && vec(a, d) == vec(b, c)

&& lengthSqr(vec(a, d)) == lengthSqr(vec(a, b)) && prependecularVec(vec(a, b), vec(a, d));

}

## Point distance to Line

double pointDistToLine(point p, point a, point b, point &c) {//line a,b

// formula: c = a + u \* ab

point ap = vec(a, p), ab = vec(a, b);

long double u = dot(ap, ab) / lengthSqr(ab);

c = translate(a, scale(ab, u)); // translate a to c

return dist(p, c); }

## Point distance to segment

// dis p to ab

double pointDistToLineSegment(point p, point a, point b, point &c) {

point ap = vec(a, p), ab = vec(a, b);

long double u = dot(ap, ab) / lengthSqr(ab);

if (u < 0.0) {// closer to a

c = point(a.X, a.Y); return dist(p, a);

} // Euclidean distance between p and a

if (u > 1.0) { // closer to b

c = point(b.X, b.Y); return dist(p, b);

} // Euclidean distance between p and b

c = translate(a, scale(ab, u)); // translate a to c //between a,b

return dist(p, c);

}

## given 2 diagonal points for the square find the other two

void square\_points(point p1, point p3, point& p2, point& p4) {

// center point

ld cx = (p1.X + p3.X) / 2.;

ld cy = (p1.Y + p3.Y) / 2.;

// half-diagonal

ld dx = (p1.X - p3.X) / 2.;

ld dy = (p1.Y - p3.Y) / 2.;

ld x2 = cx - dy, y2 = cy + dx; // second corner

ld x4 = cx + dy, y4 = cy - dx; // Fourth corner

p2 = point(x2, y2);

p4 = point(x4, y4);

return;

}

## Circle rad given 2 points and cen

bool circle2PtsRad(point p1, point p2, double r, point& c) {

double d2 = (p1.X - p2.X) \* (p1.X - p2.X) +

(p1.Y - p2.Y) \* (p1.Y - p2.Y);

double det = r \* r / d2 - 0.25;

if (det < 0.0) return false;

double h = sqrt(det);

c.real((p1.X + p2.X) \* 0.5 + (p1.Y - p2.Y) \* h);

c.imag((p1.Y + p2.Y) \* 0.5 + (p2.X - p1.X) \* h);

return true;

// to get the other center, reverse p1 and p2

}

## circleCircleIntersectionArea

ld circleCircleIntersectionArea(point cen1, ld r1, point cen2, ld r2) {

ld dis = hypot(cen1.X - cen2.X, cen1.Y - cen2.Y);

if (dis > r1 + r2)return 0;

if (dis <= fabs(r2 - r1) && r1 >= r2)

return PI \* r2 \* r2;

if (dis <= fabs(r2 - r1) && r1 < r2)

return PI \* r1 \* r1;

ld a = r1 \* r1, b = r2 \* r2;

ld ang1 = acos((a + dis \* dis - b) / (2 \* r1 \* dis)) \* 2;

ld ang2 = acos((b + dis \* dis - a) / (2 \* r2 \* dis)) \* 2;

ld ret1 = .5 \* b \* (ang2 - sin(ang2));

ld ret2 = .5 \* a \* (ang1 - sin(ang1));

return ret1 + ret2;

}

## distance between two points in arc

double calcArc(point p1, point p2, point cen) {

double d = length(vec(p1, p2));

double ang = (angle(vec(cen, p1)) - angle(vec(cen, p2))) \* 180 / PI;

if (ang < 0) ang += 360;

ang = min(ang, 360 - ang);

return r \* ang \* PI / 180;

}

## Segment and Segment intersection

bool onSegment(point p, point q, point r) {

if (q.X <= max(p.X, r.X) && q.X >= min(p.X, r.X) &&

q.Y <= max(p.Y, r.Y) && q.Y >= min(p.Y, r.Y))

return true;

return false;

}

ld orientation(point p, point q, point r) {

ld val = (q.Y - p.Y) \* (r.X - q.X) - (q.X - p.X) \* (r.Y - q.Y);

if (val == 0) return 0;

return (val > 0) ? 1 : 2;

}

bool doIntersect(point p1, point q1, point p2, point q2) {

ld o1 = orientation(p1, q1, p2);

ld o2 = orientation(p1, q1, q2);

ld o3 = orientation(p2, q2, p1);

ld o4 = orientation(p2, q2, q1);

if (fabs(o1 - o2) > EPS && fabs(o3 - o4) > EPS)

return true;

if (o1 == 0 && onSegment(p1, p2, q1)) return true;

if (o2 == 0 && onSegment(p1, q2, q1)) return true;

if (o3 == 0 && onSegment(p2, p1, q2)) return true;

if (o4 == 0 && onSegment(p2, q1, q2)) return true;

return false;

}

# 3D geometry

// give the sperical distance between 2 points using 2 angels for each (long, lat)

double spherical\_distance(double lat1, double lon1, double lat2, double lon2, double rad) {

double dlon = lon2 - lon1;

double dlat = lat2 - lat1;

double a = pow((sin(dlat / 2)), 2) + cos(lat1) \* cos(lat2) \* pow(sin(dlon / 2), 2);

double c = 2 \* atan2(sqrt(a), sqrt(1 - a));

return rad \* c;

}

## 3D Point

struct point3D{

long double x, y, z;

point3D(){};

point3D(long double x1, long double y1, long double z1){

x = x1; y = y1; z = z1;

}

bool read(){ if (cin >> x >> y >> z)return 1; return 0; }

long double dis(point3D other){

return sqrt(pow(x - other.x, 2) + pow(y - other.y, 2) + pow(z - other.z, 2));

}

};

## The volume of Triangular Pyramid

long double cosRule(long double a, long double b, long double c){

// Handle denom = 0

long double res = (b \* b + a \* a - c\*c) / (2 \* b \*a);

if (res > 1)

res = 1;

if (res < -1)

res = -1;

return res;

}

ld triangularPyramidVolume(ld AB, ld AC, ld BC, ld AD, ld BD, ld CD){

ld cos1 = cosRule(AD, BD, AB),cos2 = cosRule(BD, CD, BC),cos3 = cosRule(CD, AD, AC);

ld temp = sqrt(1 + 2 \* cos1 \* cos2 \* cos3 - cos1\*cos1 - cos2\*cos2 - cos3\*cos3);

return AD \* BD \* CD \* temp / 6;

}

long double pyramidVolume(long double ab, long double ac, long double ad,

long double bc, long double bd, long double cd) {

long double w = ab, v = ac, u = ad, U = bc, V = bd, W = cd;

long double X = (w - U + v) \* (U + v + w);

long double x = (U - v + w) \* (v - w + U);

long double Y = (u - V + w) \* (V + w + u);

long double y = (V - w + u) \* (w - u + V);

long double Z = (v - W + u) \* (W + u + v);

long double z = (W - u + v) \* (u - v + W);

long double a = sqrt(x \* Y \* Z);

long double b = sqrt(X \* y \* Z);

long double c = sqrt(X \* Y \* z);

long double d = sqrt(x \* y \* z);

long double volume = -a + b + c + d;

volume \*= a - b + c + d;

volume \*= a + b - c + d;

volume \*= a + b + c - d;

volume = sqrt(volume) / (192.0 \* u \* v \* w);

return volume;

}

# Java Scanner

static class MScanner {

    StringTokenizer st;

    BufferedReader br;

    public MScanner(InputStream system) {

        br = new BufferedReader(new InputStreamReader(system));

    }

    public MScanner(String file) throws Exception {

        br = new BufferedReader(new FileReader(file));

    }

    public String next() throws IOException {

        while (st == null  !st.hasMoreTokens())

            st = new StringTokenizer(br.readLine());

        return st.nextToken();

    }

    public String nextLine() throws IOException {

        return br.readLine();

    }

    public int nextInt() throws IOException {

        return Integer.parseInt(next());

    }

    public double nextDouble() throws IOException {

        return Double.parseDouble(next());

    }

    public char nextChar() throws IOException {

        return next().charAt(0);

    }

    public long nextLong() throws IOException {

        return Long.parseLong(next());

    }

    public int[] intArr(int n) throws IOException {

        int[]in=new int[n];for(int i=0;in;i++)in[i]=nextInt();

        return in;

    }

    public long[] longArr(int n) throws IOException {

        long[]in=new long[n];for(int i=0;in;i++)in[i]=nextLong();

        return in;

    }

    public int[] intSortedArr(int n) throws IOException {

        int[]in=new int[n];for(int i=0;in;i++)in[i]=nextInt();

        shuffle(in);

        Arrays.sort(in);

        return in;

    }

    public long[] longSortedArr(int n) throws IOException {

        long[]in=new long[n];for(int i=0;in;i++)in[i]=nextLong();

        shuffle(in);

        Arrays.sort(in);

        return in;

    }

    static void shuffle(int[]in) {

        for(int i=0;iin.length;i++) {

            int idx=(int)(Math.random()in.length);

            int tmp=in[i];

            in[i]=in[idx];

            in[idx]=tmp;

        }

    }

    static void shuffle(long[]in) {

        for(int i=0;iin.length;i++) {

            int idx=(int)(Math.random()in.length);

            long tmp=in[i];

            in[i]=in[idx];

            in[idx]=tmp;

        }

    }

    public Integer[] IntegerArr(int n) throws IOException {

        Integer[]in=new Integer[n];for(int i=0;in;i++)in[i]=nextInt();

        return in;

    }

    public Long[] LongArr(int n) throws IOException {

        Long[]in=new Long[n];for(int i=0;in;i++)in[i]=nextLong();

        return in;

    }

    public boolean ready() throws IOException {

        return br.ready();

    }

    public void waitForInput() throws InterruptedException {

        Thread.sleep(3000);

    }

}